CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge Ordinary Level

MARK SCHEME for the October/November 2014 series

4037 ADDITIONAL MATHEMATICS

4037/22 Paper 2, maximum raw mark 80

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Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Page 2	Mark Scheme	Syllabus	Paper
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1 (a)		B1	
(b)		B1	Both written or on diagram
(6)	No.in H only = $50 - x$; No in F only = $60 - x$ Sum: $50 - x + 60 - x + x + 30 - 2x = 98$ x = 14	M1 A1	Add at least 3 terms each with x involved and equate to 98 soi
2	$9x^{2} + 2x - 1 < (x + 1)^{2}$ $8x^{2} < 2 \text{ oe isw}$ $-\frac{1}{2} < x < \frac{1}{2}$	M1 A1 A1	Expand and collect terms
3	$\log_{2}(x+3) = \log_{2} y + 2 \rightarrow x + 3 = 4y$ $\log_{2}(x+y) = 3 \rightarrow x + y = 8$ $x+3 = 4(8-x)$ $5x = 29 \rightarrow x = 5.8, \text{ oe}$ $y = 2.2 \text{ oe}$	B1 B1 M1 A1 A1	Eliminate y or x from two linear three term equations

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4 (i)	$f(37) = 3 \text{ or } gf(x) = \frac{\sqrt{x-1} - 3 - 2}{2(\sqrt{x-1} - 3) - 3}$ $gf(37) = \frac{3-2}{6-3} = \frac{1}{3}$	B1 B1	
(ii)	$y = \sqrt{x-1} - 3 \rightarrow (y+3)^2 = x-1$ $(x+3)^2 + 1 = f^{-1}(x)$ oe isw	M1 A1	Rearrange and square in any order Interchange x and y and complete
(iii)	$y = \frac{x-2}{2x-3}$ $2xy-3y = x-2 \rightarrow 2xy-x = 3y-2$ $\frac{3x-2}{2x-1} = g^{-1}(x) \text{ oe}$	M1 A1	Multiply and collect like terms Interchange and complete Mark final answer
5 (i) (ii)	B = 900 $B = 500 + 400e^2 = 3455 \text{ or } 3456 \text{ or } 3460$	B1 B1	3455.6 scores B0
(iii)	$\left(\frac{dB}{dt} = \right) 80e^{0.2t}$ $t = 10 \to \frac{dB}{dt} = 80e^2 = 591(/day)$	B1 B1	awrt
(iv)	$10000 = 500 + 400e^{0.2t} \rightarrow e^{0.2t} = (23.75)$ $0.2t = \ln 23.75$ $t = 15.8 \text{ (days)}$	M1 DM1 A1	$e^{0.2t} = k$ take logs: $0.2t = \ln k$ awrt

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Points $(1, 3), (-3, -1)$ isw A1	3 term quadratic with attempt to solve both <i>x</i> or a pair both <i>y</i> or second pair
or elimination of x leads to $y^2 - 2y - 3 = 0$,	•
or elimination of x leads to $y^2 - 2y - 3 = 0$,	,
then as above	
(ii) $m^2x^2 + 10mx + 25 + x^2 = 10$ B1	
$(m^2+1)x^2+10mx+15=0$	
$\mathbf{A1}$	attempt to use discriminant on three term quadratic. Allow unsimplified
$m = \pm \sqrt{\frac{3}{2}}$ oe isw	cao ± is required
Alternative solution:	
$\frac{dy}{dx} = \frac{-x}{\sqrt{10 - x^2}} \text{ or } \frac{dy}{dx} = -\frac{x}{y}$ B1	allow unsimplified
Result:	
$y^2 = x^2 + 5y$ after inserted in $y = mx + 5$	Plining
	Eliminate <i>x</i> or <i>y</i> both
$m = \pm \frac{3}{\sqrt{6}} \text{ oe}$	0041
$m=\pm \sqrt{6}$ de	
7 (i) $v = 2\cos t + 1$ B1	mark final answer
	equate their v to zero (must be a
	differential) and attempt to solve to find an angle
$t = \frac{2\pi}{3} \text{ or } 2.09$	awrt
(iii) $t = \frac{2\pi}{3} \rightarrow x = 2\sin\left(\frac{2\pi}{3}\right) + \frac{2\pi}{3} = 3.83 \mathrm{m}$ B1	awrt
$a = -2\sin t$ R1ft	ft <i>their</i> v (2 nd differential)
2π $\sqrt{2}$ 1.73 -2	ft using <i>their</i> angle <i>t</i> in correct <i>a</i> awrt
3 4	
1 1 1 1 1 1 2 1 2 1 2 1 2 1 2 1 1	apply quotient or product rule unsimplified
	k=4 does not need to be specifically
	identified $\frac{1}{their \ k} \times \text{ original function}$

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9	$(a+3\sqrt{5})^2 = a^2 + 3\sqrt{5}a + 3\sqrt{5}a + 45$ oe	B1	anywhere
	Equate: $a^2 + a + 45 = 51$	B1	
	and $6a - b = 0$	B1	
	(a+3)(a-2)=0	M1	Attempt to solve three term quadratic with integer coefficients obtained by
	a = -3, 2 b = -18, 12	A1 A1	equating coeffs Both as correct or one correct pair Both bs correct
10 (i)	$\sec x \csc x = \frac{1}{\cos x \sin x}$	B1	anywhere
	$\cot x = \frac{\cos x}{\sin x}$	B1	anywhere
	$LHS = \frac{1 - \cos^2 x}{\cos x \sin x} \text{ oe}$	B1ft	correct addition of their terms
	$= \frac{\sin^2 x}{\cos x \sin x} = \tan x \qquad AG$	B1	use of identity and cancel
(ii)	$3\cot x - \cot x = \tan x \to 2\cot x = \tan x$	M1	equate and collect like terms, allow sign errors
	$\tan^2 x = 2$ oe x = 54.7, 125.3, 234.7, 305.3	A1 A1	2 values
	x = 54.7, 125.3, 254.7, 305.5	A1	only 2 more values. awrt
11 (i)	Area of sector = $\frac{1}{2} \times x^2 \times 0.8 = 0.4x^2 \text{ cm}^2$	B1	anywhere
	$SR = 5\sin 0.8 (= 3.59)$ or	B1	SR may be seen in stated $\frac{1}{2}ab\sin C$
	$OR = 5\cos 0.8 (= 3.48)$		
	Area of triangle =		
	$\frac{1}{2}5\cos 0.8 \times 5\sin 0.8 = 6.247 \text{cm}^2$	M1	insert correct terms into correct area
	$\begin{bmatrix} 2 \\ 0.08x^2 = 6.247 \end{bmatrix}$	A1	formulae
	x = 8.837 cm AG	A1	
(ii)	SQ = 8.84 - 5 (= 3.84 cm)		
	$PR = 8.84 - 5\cos 0.8 (= 5.35 \text{ or } 5.36 \text{cm})$	B1	two lengths from SQ, PR, PQ awrt
	$PQ = 8.84 \times 0.8 (= 7.07 \text{ cm})$	B1	third length awrt
	Perimeter = 19.84 to 19.86 cm or rounded to 19.8 or 19.9	B1	sum
(iii)	Area $PQSR = 4 \times 6.247$	M1	
	$=25\mathrm{cm}^2$	A1	24.95 to 25

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12 (i)	$f(2) = 3(2^3) - 14(2^2) + 32 = 0$ Or complete long division	B1	
(ii)	$f(x) = (x-2)(3x^2 - 8x - 16)$	M1 A1 M1	$3x^2$ and 16 8x and correct signs Factorise three term quadratic
	f(x) = (x-2)(x-4)(3x+4)	A1	Table to the quantum q
(iii)	x = 2, 4	B 1	
(iv)	$\int 3x - 14 + \frac{32}{x^2} dx = 1.5x^2 - 14x - \frac{32}{x} (+c)$	B1 B1	first 2 terms third term correct unsimplified
	Area = $\left[1.5x^2 - 14x - \frac{32}{x} \right]_2^4$	M1	Limits of 2 and 4 and subtract
	= (-) 2	A1	