



# Cambridge International AS & A Level

CANDIDATE  
NAME

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CENTRE  
NUMBER

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## FURTHER MATHEMATICS

9231/12

Paper 1 Further Pure Mathematics 1

May/June 2020

2 hours

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Blank pages are indicated.

1 Let  $a$  be a positive constant.

(a) Sketch the curve with equation  $y = \frac{ax}{x+7}$ .

[2]

- (b) Sketch the curve with equation  $y = \left| \frac{ax}{x+7} \right|$  and find the set of values of  $x$  for which  $\left| \frac{ax}{x+7} \right| > \frac{a}{2}$ .  
[4]

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2 The cubic equation  $6x^3 + px^2 - 3x - 5 = 0$ , where  $p$  is a constant, has roots  $\alpha, \beta, \gamma$ .

(a) Find a cubic equation whose roots are  $\alpha^2, \beta^2, \gamma^2$ . [3]

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(b) It is given that  $\alpha^2 + \beta^2 + \gamma^2 = 2(\alpha + \beta + \gamma)$ .  
(i) Find the value of  $p$ . [3]

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(ii) Find the value of  $\alpha^3 + \beta^3 + \gamma^3$ . [2]

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3 The curve  $C$  has equation  $y = \frac{x^2}{2x+1}$ .

(a) Find the equations of the asymptotes of  $C$ . [3]

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(b) Find the coordinates of the stationary points on  $C$ . [3]

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(c) Sketch *C*.

[3]

- 4 (a) By first expressing  $\frac{1}{r^2-1}$  in partial fractions, show that

$$\sum_{r=2}^n \frac{1}{r^2-1} = \frac{3}{4} - \frac{an+b}{2n(n+1)},$$

where  $a$  and  $b$  are integers to be found.

[5]

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