

CANDIDATE
NAME

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CENTRE
NUMBER

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CANDIDATE
NUMBER

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FURTHER MATHEMATICS

9231/13

Paper 1

May/June 2019

3 hours

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF10)

READ THESE INSTRUCTIONS FIRST

Write your centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions in the space provided. If additional space is required, you should use the lined page at the end of this booklet. The question number(s) must be clearly shown.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of a calculator is expected, where appropriate.

Results obtained solely from a graphic calculator, without supporting working or reasoning, will not receive credit.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

This document consists of **23** printed pages and **1** blank page.



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2 The curve C has polar equation $r^2 = \ln(1 + \theta)$, for $0 \leq \theta \leq 2\pi$.

(i) Sketch C .

[2]

(ii) Using the substitution $u = 1 + \theta$, or otherwise, find the area of the region bounded by C and the initial line, leaving your answer in an exact form. [5]

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6 The curve C has equation

$$y = \frac{x^2}{kx - 1},$$

where k is a positive constant.

(i) Obtain the equations of the asymptotes of C . [3]

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(ii) Find the coordinates of the stationary points of C . [3]

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(iii) Sketch *C*.

[3]

- 9 A cubic equation $x^3 + bx^2 + cx + d = 0$ has real roots α , β and γ such that

$$\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma} = -\frac{5}{12},$$

$$\alpha\beta\gamma = -12,$$

$$\alpha^3 + \beta^3 + \gamma^3 = 90.$$

- (i) Find the values of c and d . [3]

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- (ii) Express $\alpha^2 + \beta^2 + \gamma^2$ in terms of b . [2]

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- (iii) Show that $b^3 - 15b + 126 = 0$. [4]

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OR

The positive variables y and t are related by

$$y = a^t,$$

where a is a positive constant.

- (i) (a) By differentiating $\ln y$ with respect to t , show that $\frac{dy}{dt} = a^t \ln a$. [3]

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- (b) Write down $\frac{d^2y}{dt^2}$. [1]

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- (ii) Determine the set of values of a for which the infinite series

$$y + \frac{dy}{dt} + \frac{d^2y}{dt^2} + \frac{d^3y}{dt^3} + \dots$$

is convergent. [3]

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