#### **CAMBRIDGE INTERNATIONAL EXAMINATIONS**

GCE Advanced Subsidiary Level and GCE Advanced Level

## MARK SCHEME for the October/November 2013 series

# 9709 MATHEMATICS

9709/63 Paper 6, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



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### **Mark Scheme Notes**

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol <sup>↑</sup> implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously 'correct' answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
MR PA	Misread  Premature Approximation (resulting in basically correct work that is insufficiently accurate)
	Premature Approximation (resulting in basically correct work that is insufficiently

### **Penalties**

- MR −1 A penalty of MR −1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become 'follow through √ marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR −2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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1	bars are not touching oe	B1		Sensible reason involving not touching, no gaps, class boundaries, group data not continuous (may be the negative)
	Area not rep by frequency, not used fd, not labelled fd	B1	2	Must be frequency density oe. Wrong height not sufficient. (Best 2 reasons awarded)
<b>2</b> P(1:	$3.6 < X < 14.8) = P\left(\frac{13.6 - 14}{0.52} < z < \frac{14.8 - 14}{0.52}\right)$	M1		Standardising 1 expression, no cc, no sq rt, no sq, $\pm$ , mean on num.
	$= P(-0.7692 < z < 1.538)$ $= \Phi(1.538) - [1 - \Phi(0.7692)]$	M1		$\Phi$ 1 + $\Phi$ 2 – 1 (indep) oe ( $\Phi$ 2 – $\Phi$ 1 if cc used)
	= 0.9380 - [1 - 0.7791] = 0.7171	A1		Correct probability rounding to 0.72 here
	$P(8) = (0.7171)^8 (0.2829)^2_{10} C_8$	M1		Binomial expression 10C8 $p^8q^2$ , $\Sigma p + q = 1$ , any $p$
	= 0.252	A1	5	Correct answer (rounding to 0.252)
3	(i) $(p=)0.85$	В1		(p = )0.85 oe seen anywhere
	$P(<12) = 1 - P(12, 13, 14)$ $= 1 - [(0.85)^{12}(0.15)^{2}_{14}C_{12} + (0.85)^{13}(0.15)_{14}C_{13} + (0.85)^{14}]$ $= 1 - 0.6479$ $= 0.352$		3	Summing 2 or 3 consistent bin probs, any $p < 1$ , $n = 14$ (or summing 12 or 13 consistent bin probs)  Correct answer
		A1		
	(ii) $(0.85)^n \ge 0.1$ $n \le 14.2$ n = 14	M1 M1 A1	3	Eqn or inequality in 0.85(or 0.15), <i>n</i> , 0.1, <i>n</i> as a power Attempt to solve (can be implied) if <i>n</i> a power Correct answer – must be equals, not approx. MR allowed for 0.01, M1M1A0 max.
4	(i) (220×20 + 118×25)/45 = 163	M1 A1	2	Mult by 20 and 25 and dividing their sum by 45 Correct answer, 163.3 or 490/3 oe acceptable
	(ii) $\Sigma x_o^2 / 20 - 220^2 = 32^2$ $\Sigma x_o^2 = 988480$	M1 A1		Subst in correct variance formula Correct $\Sigma x_0^2$
	$\sum x_l^2 / 25 - 118^2 = 12^2$ $\sum x_l^2 = 351700$	A1		correct $\Sigma x_1^2$
	$\Sigma x_o^2 + \Sigma x_l^2 = 1340180$ New var = 1340180/45 - (7350/45) <sup>2</sup> = 3100 - 3120	M1 A1	5	Subst their combined results in correct var formula Correct answer

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5 (a)	P( $X < q + 82$ ) = 0.72 z = 0.583 $\frac{\pm q}{7.4}$ or $\frac{\pm 2q}{7.4}$ = z or probabilty (o.e.)	M1 M1		Rounding to $\pm$ 0.58 or $\pm$ 0.15 seen Standardising, no cc, no sq, no sq rt
	q = 4.31	A1	3	correct answer
(b)	$\frac{0.5\mu - \mu}{\sigma} = \frac{\pm 0.5\mu}{\sigma}$	M1		Standardising attempt some $\mu/\sigma$ allow cc, sq rt, sq Can be implied
	$\frac{0.2\sigma^2}{\sigma} = -0.2\sigma = -0.580$	B1 M1		$\pm0.580$ seen (accept $\pm0.58)$ substituting to eliminate $\mu$ or $\sigma$ , arriving at numerical solution, any z value or probability – not dependent
	$\sigma = 2.90$ $\mu = 3.36$	A1	4	both answers correct, accept 2.9
6 (i)	8! 3!2!2!	M1		8! Divided by at least one of 3!2!2! oe
	= 1680	A1	2	Correct answer
(ii)	5! = 120	M1 A1	2	5! Seen (not added, may be divided/multipled) Correct answer
(iii)	<u>5!4!</u> <u>3!2!2!</u>	B1		5! Or 4! Seen in sum or product in numerator (denominator may by 1)
		M1		$\frac{k5!4!}{3!2!2!}$ in a numerical expression
	= 120	A1	3	Correct final answer
(iv)	TA, TE, = 8 ways	M1		Summing 2 options (could be lists)
	GGG with A, E, R, T = 4 ways  Total = 12 ways	A1 A1	3	1 correct option  Correct answer

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7 (i) $P(same) = P(1, 1) + P(3, 3) + P(5, 5)$ $= \frac{2}{9} \times \frac{1}{8} + \frac{4}{9} \times \frac{3}{8} + \frac{3}{9} \times \frac{2}{8}$ $= 5/18 (0.278)$ Alt. method: $\frac{2C2 + 4C2 + 3C2}{9C2}$ or $\frac{2 \times 1 + 3 \times 4 + 2 \times 3}{9C2 \times 2}$ oe  M1 Summing 3 two-factor options  Multiplying terms by one less in the or denominator  A1 3 Correct answer  M1 for numerator, M1 for denominator	he numerator
or denominator $= 5/18 (0.278)$ Alt. method: $\frac{2C2+4C2+3C2}{9C2}$ M1 for numerator, M1 for d A1 correct answer	he numerator
Alt. method: $ \frac{2C2+4C2+3C2}{9C2} $ M1 for numerator, M1 for d A1 correct answer	
$\frac{2C2+4C2+3C2}{9C2}$ M1 for numerator, M1 for d A1 correct answer	
JC2^2	enominator,
(ii) $P(5,\overline{5}) + P(\overline{5},5)$ M1 Mult 2 probs whose numerators sure Summing 2 options or mult by 2 (may be 4 options)	m to 9 o.e.
$= \frac{3}{9} \times \frac{6}{8} + \frac{6}{9} \times \frac{3}{8} = \frac{36}{72} = \frac{1}{2} \text{ or } 0.5$ A1 3 Correct answer	
Alt. method: $\frac{6C1 \times 3C1(\times 2)}{9C2(\times 2)}  oe$ M1 for numerator, M1 for A1 correct answer	denominator,
(iii) $P(5 \cap \overline{5}) = \frac{3}{9} \times \frac{6}{8} = \frac{1}{4}$ M1 Attempt at P(5 and not 5) seen as n denominator of a fraction	numerator or
$P(\overline{5}) = \frac{1}{4} + \frac{6}{9} \times \frac{5}{8} = 48/72 = 0.6666$ M1 Attempt at P(not 5) sum of 2 two-fine seen anywhere	actor terms
$P(5_1 \overline{5}_2) = \frac{1/4}{48/72} = 3/8$ A1 Correct $P(\overline{5})$ as numerator or denoting fraction	ominator
= 0.375 A1 4 Correct answer	
(iv) $x = 0   1   2   P(X = x)   5/12   1/2   1/12$ B1 Values 0, 1, 2 seen in table with at	least 1 prob
$P(0) = P(\overline{5}, \overline{5}) = \frac{6}{9} \times \frac{5}{8} = 30/72 $ (5/12) B1 Correct P(0) unsimplified (0.4166)	
P(1) = 0.5  from part (ii)	
$P(2) = 6/72 (1/12) (0.0833)$ from part (i) B1ft 3 If $x=0,1,2(,3)$ ft $\Sigma p = 1$ , no -ve probabilities <1	e values, all