

# **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
CAMPRIDGE	NTERNATIONAL MATHEMATICS		0607/41

#### CAMBRIDGE INTERNATIONAL MATHEMATICS

Paper 4 (Extended)

October/November 2017

2 hours 15 minutes

Candidates answer on the Question Paper.

Additional Materials: Geometrical Instruments

**Graphics Calculator** 

### **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, glue or correction fluid.

You may use an HB pencil for any diagrams or graphs.

DO NOT WRITE IN ANY BARCODES.

#### Answer all the questions.

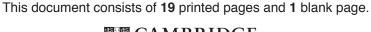
Unless instructed otherwise, give your answers exactly or correct to three significant figures as appropriate. Answers in degrees should be given to one decimal place.

For  $\pi$ , use your calculator value.

You must show all the relevant working to gain full marks and you will be given marks for correct methods, including sketches, even if your answer is incorrect.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 120.





# Formula List

For the equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Curved surface area, A, of cylinder of radius r, height h.

$$A = 2\pi rh$$

Curved surface area, A, of cone of radius r, sloping edge l.

$$A = \pi r l$$

Curved surface area, A, of sphere of radius r.

$$A = 4\pi r^2$$

Volume, V, of pyramid, base area A, height h.

$$V = \frac{1}{3}Ah$$

Volume, V, of cylinder of radius r, height h.

$$V = \pi r^2 h$$

Volume, V, of cone of radius r, height h.

$$V = \frac{1}{3}\pi r^2 h$$

Volume, V, of sphere of radius r.

$$V = \frac{4}{3}\pi r^3$$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$Area = \frac{1}{2}bc \sin A$$

# Answer all the questions.

1

The	ese ar	e 12 of	Stefan's	recent	homew	ork sco	ores.							
		10	16	18	11	18	15	8	18	13	9	12	11	
(a)	Fine	d												
	(i)	the mo	ode,											
												• • • • • • • • • • • • • • • • • • • •		 [1]
	(ii)	the rai	nge,											
													•••••	 [1]
	(iii)	the me	edian,											
														 [1]
	(iv)	the me	ean,											
														 [1]
	(v)	the int	erquart	ile rang	ge.									
												•••••		 [2]
(b)	The	teache	r wants	to com	pare Ste	efan's s	cores w	ith tho	se of an	other s	tudent	in the	class.	
	Exp	lain wh	y the m	ode is 1	not the l	best val	ue to us	se to re	present	Stefan	's scor	es.		
	••••	•••••			•••••	•••••	•••••					•••••		 
														 [1]

-	Two	banks pay	interest in the following ways.								
]	Ban	k A	Simple interest at a rate of 2.5% per year for the first rate of 1.5% per year for each year after that.	st year and then compound interest at a	ì						
]	Ban	k B	Simple interest at 1.6% per year.								
(a) Cherie in			evested \$3000 in Bank A on 1st January 2016.								
		Find how	much the investment will be worth on 1st January 20	019.							
				\$[	31						
	(b)	Dieter inv	vested \$3000 in Bank B on 1st January 2016.	Ψ [.	ر ر						
•	(6)		much the investment will be worth on 1st January 20	019							
		i ilia ilow	much the investment will be worth on 1st sundary 20	017.							
				\$[	3]						
(	(c)	Show that	t Cherie's investment will be the first to be worth \$35	500.							

[4]

(a)	The <i>n</i> th term of a sequence is $n^2 + 3n$ .
	Find the first four terms of this sequence.
	,, ,
(b)	These are the first four terms of another sequence.
	5 7 9 11
	(i) Write down the next two terms.
	, ,
	(ii) Find the <i>n</i> th term of this sequence.
	[2]
(c)	Using the sequences in <b>part (a)</b> and <b>part (b)</b> , or otherwise, find the <i>n</i> th term of this sequence.
	14, 24, 36, 50,
	Write your answer as simply as possible.

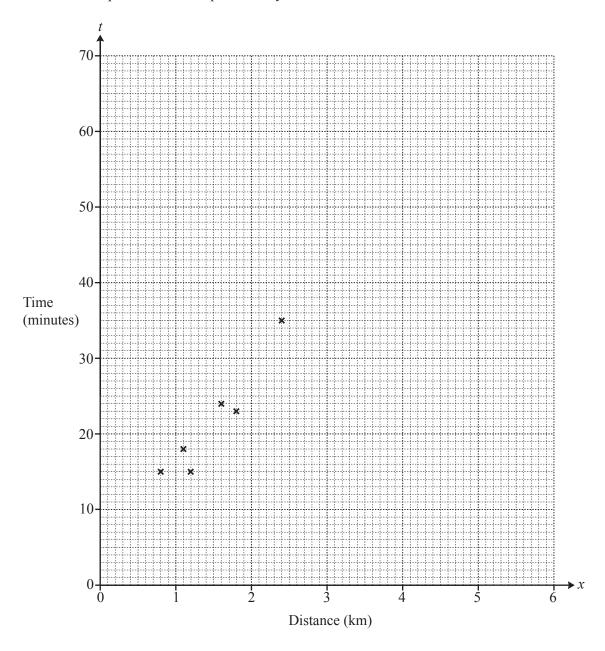
.....[2]

4 The table shows the distance that each of 12 students lives from school and the time they each take to get to school

Distance (x km)	0.8	1.1	1.2	1.6	1.8	2.4	2.8	3.1	3.5	4.2	4.7	5.1
Time (t minutes)	15	18	15	24	23	35	37	35	45	48	52	63

(a) Complete the scatter diagram.

The first six points have been plotted for you.

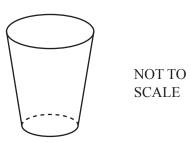


[2]

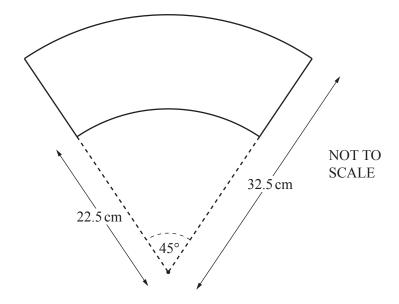
**(b)** What type of correlation is shown by the scatter diagram?

(c) (i)	Find the equation of the regression line in the form $t = mx + c$ .
	$t = \dots [2]$
(ii)	Use your answer to <b>part</b> (c)(i) to estimate the time taken to get to school for a student who lives 2.2 km from school.
	min [1]
(iii)	Why would it not be sensible to use your answer to <b>part</b> (c)(i) to estimate the time taken to get to school for a student who lives 10 km from school?
	[1]

5 The diagram shows a paper cup.



The curved surface of the cup is made from a sector of a circle with a smaller sector cut from it, as shown below.

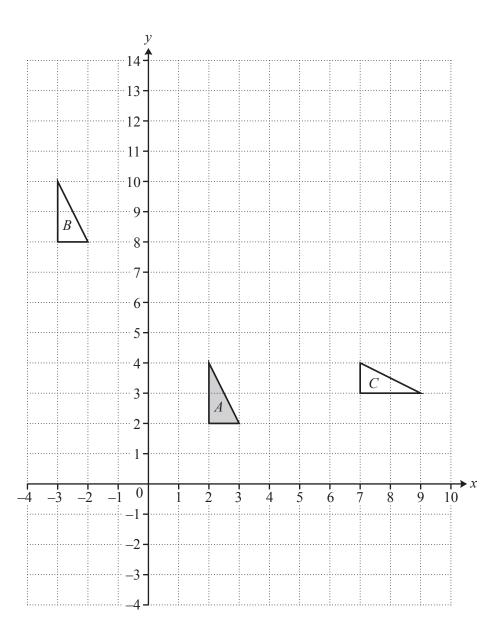


The small sector has radius  $22.5\,\mathrm{cm}$  and the large sector has radius  $32.5\,\mathrm{cm}$ . The sectors have the same centre and both have sector angle  $45^\circ$ .

(a) Show that the radius of the base of the cup is 2.81 cm, correct to 2 decimal places.

[3]

(b)	Find the total area of the paper that makes the cup, including the circular base.
	2 ге
	cm <sup>2</sup> [5]
(c)	A mathematically similar cup holds 8 times as much liquid as this cup.
(c)	A mathematically similar cup holds 8 times as much liquid as this cup.  Find the total area of the paper that makes the larger cup.
(c)	
(c)	
(c)	Find the total area of the paper that makes the larger cup.
(c)	
(c)	Find the total area of the paper that makes the larger cup.



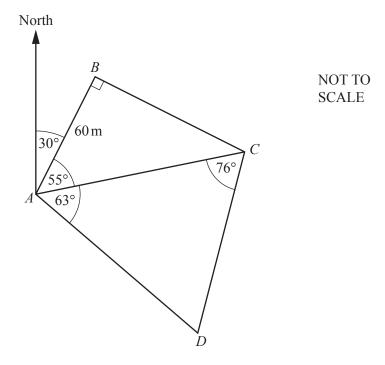
(a)	Describe fully the <b>single</b> transformation that maps triangle $A$ onto triangle $B$ .

- (b) On the grid, draw the image of triangle A after a stretch with scale factor 3 and invariant line the x-axis. [2]
- (c) Triangle A can be mapped onto triangle C by a rotation followed by a reflection.Complete the following to fully describe the two transformations.

Reflection [3]

Javi	ier starts a journey at 2250.		
(a)	For the first part of the journey he drives for 2 hours 45 minutes a	at 70 km/h.	
	Find the distance he travels.		
		km	[3]
(b)	Javier then stops for 30 minutes. He then drives the remaining 180 km of his journey at 85 km/h.		
	(i) Find his average speed for the whole journey.		
		km/h	[4]
	(ii) Find the time he arrives at his destination.		
			[2]
			[2]

**8** *ABC* and *ACD* are two triangular fields.



(a) Find the bearing of B from C.

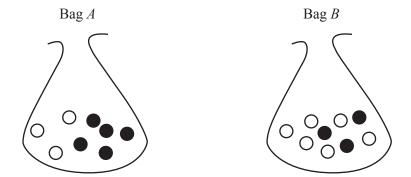
[3]
 1-

**(b)** Calculate AC and show that it rounds to 104.6 m, correct to 1 decimal place.

[3]

(c)	Calculate the total area of the two fields.	
		m <sup>2</sup> [6]
(d)	Maria walks in a straight line from <i>D</i> towards <i>A</i> . She stops when she is at her closest point to <i>C</i> .	
	Calculate her distance from <i>C</i> .	
		m [2]
	·	m [2]

9 Two bags each contain white balls and black balls only.

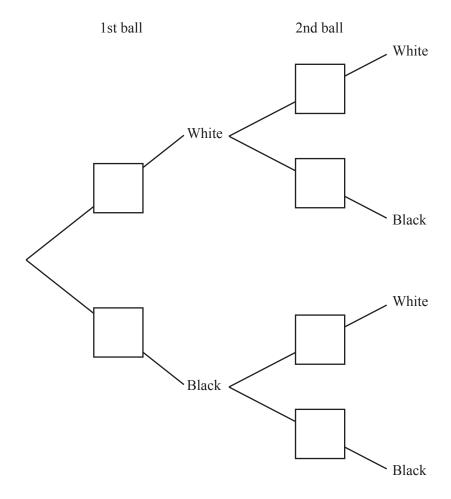


Bag *A* contains 3 white balls and 5 black balls. Bag *B* contains 6 white balls and 3 black balls.

A ball is picked at random from the 8 balls in Bag A.

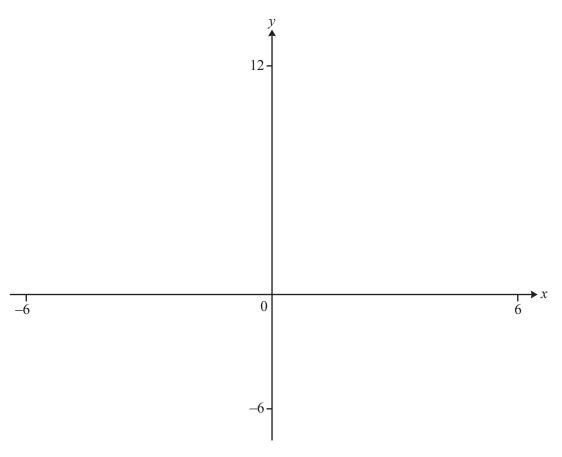
- If it is white, the ball is not replaced and a second ball is picked at random from **Bag** A.
- If it is black, a second ball is picked at random from the 9 balls in **Bag** B.

# (a) Complete the tree diagram.



(b)	Finc	d the probability that
	(i)	both balls are white,
	(ii)	exactly one of the two balls is black.
		[3]

10	(a)	Mak	xe y the subject of 3x + y = 8.
			y =  [1]
	<b>(b)</b>	The	line $3x + y = 8$ intersects the curve $x^2 + y^2 = 25$ at two points.
		(i)	Use substitution to show that $10x^2 - 48x + 39 = 0$ .
			[3]
		(ii)	Solve the equation $10x^2 - 48x + 39 = 0$ and find the co-ordinates of the two points of intersection. Show all your working.
			()
			(, ,) [5]



$$f(x) = \frac{2x^2 + 3x}{(x+2)(3-x)}$$

(a)	On the diagram,	sketch the graph of	y = f(x)	for values of $x$ between $-6$ and $6$ .	[3]
-----	-----------------	---------------------	----------	--	-----

**(b)** Find the co-ordinates of the local minimum.

(	)	$\Gamma \cap I$
(	,)	$\lfloor 2 \rfloor$

(c) Find the equations of the two asymptotes that are parallel to the y-axis.

(d) 
$$g(x) = 3x + 2$$

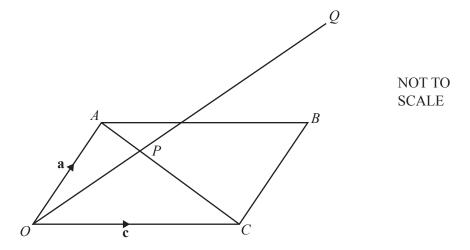
Solve.

**(i)** 
$$f(x) = g(x)$$

**(ii)** 
$$f(x) > g(x)$$

			10		
12	f(x) = 5 - 3x	g(x) = 2x + 3			
	(a) Solve $f(x) = 11$ .				
	<b>(b)</b> Find $f^{-1}(x)$ .		<i>x</i> =	=	[2]
	(c) Solve $f(x) \times g(x)$	y=0.	$f^{-1}(x) =$	=	[2]
					[2]
	(d) Simplify.				
	(i) $g^{-1}(g(x))$				
	(ii) $f(f(x)) + g(x)$				[1]
	2 4				[3]

.....[3]



OABC is a parallelogram and OPQ is a straight line.

P divides AC in the ratio 1:2. P divides OQ in the ratio 1:2.

 $\overrightarrow{OA} = \mathbf{a}$  and  $\overrightarrow{OC} = \mathbf{c}$ .

(a)	Find these vectors in terms of a and/or c
	Give each answer in its simplest form.

(i)	ΑĆ
(1)	210

	Г1	1	
•••••	$\Gamma_1$	I	

(ii) 
$$\overrightarrow{OP}$$

(iii) 
$$\overrightarrow{CQ}$$

(b) Use your answer to part(a)(iii) to complete the statement.

The points C, B and Q are [1]

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