

## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/42 October/November 2016

Paper 4 Paper 4 (Extended) MARK SCHEME Maximum Mark: 120

Published

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## Abbreviations

| awrt | answers which round to     |
|------|----------------------------|
| cao  | correct answer only        |
| dep  | dependent                  |
| FT   | follow through after error |
| isw  | ignore subsequent working  |
| oe   | or equivalent              |
| SC   | Special Case               |
| nfww | not from wrong working     |
| soi  | seen or implied            |

| Qu | estion        | Answer           | Mark | Part Marks   |
|----|---------------|------------------|------|--|
| 1  | (a)           | 171              | 1    |  |
|    | (b)           | 10               | 1    |  |
|    | (c)           | 172              | 1    |  |
|    | ( <b>d</b> )  | 4                | 2    | <b>B1</b> for 170 or 174 seen  |
|    | (e)           | 172.1            | 2    | <b>M1</b> for attempt at $\sum fx$ soi by 24099 or 172 or 172.1  |
| 2  | (a)           | 2.83 or 2.828    | 3    | <b>B2</b> for $\sqrt{8}$ or $2\sqrt{2}$ final answer<br>or <b>M2</b> for $2^2 + 2^2$<br>or <b>M1</b> for correct sketch            |
|    | ( <b>b</b> )  | 225 cao          | 2    | <b>B1</b> for 45 soi by e.g. 135<br>If 0 scored <b>SC1</b> for 224.9 to 225.1  |
|    | (c)           | 8 cao            | 2    | <b>M1</b> for $2 \times 3 + 0.5 \times 2 \times 2$ oe  |
| 3  | (a)           | Positive         | 1    |  |
|    | (b) (i)       | 12.15            | 1    |  |
|    | ( <b>ii</b> ) | 66               | 1    |  |
|    | (c) (i)       | y = 37.2 + 2.37x | 2    | Range 37.20 to 37.21 and 2.369 to 2.370<br><b>B1</b> for $37.2 + kx$ , or $a + 2.37x$ ,<br>If 0 scored, <b>SC1</b> for $37 + 2.4x$ |
|    | ( <b>ii</b> ) | 82 or 82.2       | 1    | <b>FT</b> their (i)  |

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| Qu | estion       | Answer  | Mark | Part Marks   |
|----|--------------|---|------|--|
| 4  | (a)          | 48  | 1    |  |
|    | (b)          | 84  | 2    | <b>FT</b> (180 – 2 × <i>their</i> (a)), <i>their</i> (a) $\neq$ 45<br><b>M1</b> for (180 – 2 × <i>their</i> (a)) <i>their</i> (a) $\neq$ 45                                  |
|    | (c)          | 42  | 1    | <b>FT</b> <i>their</i> (b) $\div 2$  |
|    | ( <b>d</b> ) | 69 cao  | 2    | <b>B1</b> for angle <i>OBC</i> or <i>OAC</i> = 21 or angle $ABC = 69$  |
|    | (e)          | 55.5  | 2    | <b>FT</b> <i>their</i> (d)<br><b>M1</b> for (180 – <i>their</i> (d)) ÷ 2   |
| 5  | (a)          | 36.7 or 36.68 to 36.69  | 2    | <b>B1</b> for at least 3 of (7.5, 17.5, 30, 42.5, 70) soi<br>by 4402.5<br>Accept 37.2 or 37.18 to 37.19 for full marks and<br>3 of (8, 18, 30.5, 43, 70.5) soi for <b>B1</b> |
|    | (b)          | 0.8, 3.6, 2.6, 2.7, 1.47 or 1.466 to 1.467, 0.7                   | 3    | <b>B2</b> for 4 or 5 correct<br>or <b>B1</b> for 2 or 3 correct  |
| 6  | (a)          | Reflection $y = x$  | 2    | <b>B1</b> for each   |
|    | (b)          | Rotation, centre (2, 3)<br>90 [anticlockwise] or 270<br>clockwise | 2    | <b>B1</b> for each   |
|    | ( <b>c</b> ) | Translation $ \begin{pmatrix} -4 \\ 3 \end{pmatrix} $             | 2    | <b>B1</b> for each   |
|    | ( <b>d</b> ) | Enlargement, centre (0, 0)  | 2    | Allow reduction  |
|    |              | [SF] $\frac{1}{3}$ oe   |      | <b>B1</b> for each   |
| 7  |              | Correctly equating one set of coefficients                        | M1   | Equation $x = $ or $y = $ from one equation  |
|    |              | coentcients   |      | Note – a correct sketch showing intersection in third quadrant scores <b>M2</b> (other sketches may score the <b>M1</b> for $y = \dots$ seen)                                |
|    |              | Correct method to eliminate one variable                          | M1   | Correct substitution into other equation   |
|    |              | x = -2<br>$y = -\frac{1}{2}$                                      | B2   | <b>B1</b> for each<br>If zero scored <b>SC1</b> for correct substitution into<br>one of original equations and evaluation to find<br>other variable                          |

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| Qu | estion         | Answer   | Mark | Part Marks  |
|----|----------------|--|------|---|
| 8  | (a)            | $\frac{\sqrt{8}}{3}$ or $\frac{2\sqrt{2}}{3}$ or $\sqrt{\frac{8}{9}}$  | 3    | <b>M2</b> for $\frac{\sqrt{3^2 - 1^2}}{3}$<br>or <b>M1</b> for $3^2 - 1^2$  |
|    |                |  |      | If 0 scored, <b>SC1</b> for 0.943 or 0.9428 or $\sqrt{0.889}$   |
|    | (b) (i)        | $[\cos B] = \frac{9^2 + 10^2 - 11^2}{2 \times 9 \times 10} \text{ oe}$ | 2    | <b>M1</b> for $11^2 = 9^2 + 10^2 - 2 \times 9 \times 10 \times \cos B$  |
|    | ( <b>ii</b> )  | $0.5 \times 9 \times 10 \times their \text{ exact (a)}$                | M2   | M1 for $0.5 \times 9 \times 10 \times their$ (a)<br>(their (a) must be < 1)   |
|    |                | Leading to $30\sqrt{2}$  | A1   | Cancelling seen or $\frac{180\sqrt{2}}{6}$ or $\frac{90\sqrt{2}}{3}$ or $\frac{60\sqrt{2}}{2}$<br>seen  |
| 9  | (a)            | 21.5 or 21.45 to 21.46   | 2    | <b>M1</b> for $100 - \pi \times 5^2$ oe   |
|    | (b) (i)        | 5.77 or 5.773 to 5.774   | 2    | <b>M1</b> for $\tan 60 = \frac{10}{x}$ oe   |
|    | ( <b>ii</b> )  | 21.5 or 21.54 to 21.55   | 2    | <b>M1</b> for $10 + 2 \times their$ (b)(i) oe<br>or $10 + \frac{10}{\sin 60}$ oe  |
|    | ( <b>iii</b> ) | 100 to 101.0 nfww  | 4    | <b>M3</b> for $0.5 \times 10 \times their$ (b)(i) + $0.5 \times 10 \times their$<br>(b)(i) + $0.5 \times 10 \times 10 \sin 60$ oe<br>or <b>M2</b> for any 2 of these<br>or <b>M1</b> for any 1 of these                   |
|    |                |  |      | OR  |
|    |                |  |      | <b>M3</b> for $0.5 \times (their(b)(ii))^2 \times \sin 60 - 10^2$ oe<br>or <b>M2</b> for $0.5 \times (their(b)(ii))^2 \times \sin 60$ oe<br>or <b>M1</b> for <i>their</i> attempt at area of triangle<br><i>ABC</i> - 100 |

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| Que | estion       | Answer   | Mark   | Part Marks   |
|-----|--------------|--|--------|--|
| 10  | (a)          | Fully correct curve                                  | 3      | <b>B2</b> for both branches but with serious 'curl back'<br>and/or overlap.<br>or <b>B1</b> for 1 branch   |
|     | (b)          | $\begin{array}{l} x = 2\\ y = 3 \end{array}$         | 2      | <b>B1</b> for each   |
|     | ( <b>c</b> ) | [x = ] -4<br>[x = ] 3                                | 2      | <b>B1</b> for each   |
|     | (d)          | $\begin{array}{l} x < -4 \\ 2 < x < 3 \end{array}$   | 1<br>2 | <b>FT</b> <i>their</i> –4 from (c)<br><b>FT</b> <i>their</i> 2 from (b) and <i>their</i> 3 from (c)<br><b>B1</b> for each  |
|     | (e) (i)      | Translation $ \begin{pmatrix} 2 \\ 0 \end{pmatrix} $ | 2      | <b>B1</b> for each   |
|     | (ii)         | Translation $ \begin{pmatrix} 0 \\ 3 \end{pmatrix} $ | 2      | <b>B1</b> for each   |
| 11  | (a)          | $\frac{216}{n^3 \text{ oe}}$                         | 1<br>1 |  |
|     | (b)          | $43 n^2 + n + 1$ oe                                  | 1<br>3 | <b>M2</b> for $pn^2 + qn + c$ $p, q, c \neq 0$<br>or <b>M1</b> for second differences = 2<br>or $pn^2 + c$ or $pn^2 + qn$  |
|     | (c)          | 173<br>$n^{3} - n^{2} - n - 1$ oe                    | 1<br>3 | FT their (a) – their (b)<br>FT their (a) – their (b)<br>M2 for $pn^3 + qn^2 + rn + c$ $p, q, r, c \neq 0$<br>or $n^3 - their$ (b)<br>or M1 for third differences = 6<br>or for $pn^3 + qn^2 + c$<br>or $pn^3 + qn^2 + rn$ or $pn^3 + rn + c$ |

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| Que | estion        | Answer  | Mark | Part Marks   |
|-----|---------------|---|------|--|
| 12  | (a) (i)       | 144π  | 2    | <b>M1</b> for $\frac{2}{3} \times \pi \times 6^3$  |
|     | (ii)          | 108π  | 2    | <b>M1</b> for $2\pi \times 6^2 + \pi \times 6^2$<br>If 0 scored <b>SC1</b> for $72\pi$   |
|     | (b) (i)       | 12 or 11.99 to 12.01 nfww   | 3    | M2 for $\frac{their(a)(i) \times 16}{\frac{4}{3}\pi}$ oe   |
|     |               |   |      | or <b>M1</b> for $\frac{4}{3} \times \pi \times r^3 = their(a)(i) \times 16$   |
|     | ( <b>ii</b> ) | 1 : 3 or $\frac{1}{3}$ : 1 cao nfww                                       | 3    | <b>M2</b> for $4 \times \pi \times (their(b)(i))^2 : 16 \times their(a)(ii)$ oe<br>or <b>M1</b> for $4 \times \pi \times (their(b)(i))^2$<br>or $16 \times their(a)(ii)$ |
| 13  | (a)           | $\frac{p^3q^2}{6}$ final answer   | 3    | M1 for correct use of $a \log b$<br>M1 for correct use of $\log a \pm \log b$  |
|     | (b) (i)       | 1.29 or 1.292   | 3    | <b>M2</b> for $\frac{\log 6}{\log 4}$ or $\log_4 6$ or sketch of $y = 4^x$   |
|     |               |   |      | and $y = 6$ oe<br>or <b>M1</b> for $x\log 4 = \log 6$ or sketch of $y = 4^x$   |
|     | (ii)          | $6x^2 - 5x - 7 = 0$   | B2   | or <b>B1</b> for 3 terms correct in expansion $6x^2 - 9x + 4x - 6$   |
|     |               | $x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4 \times 6 \times (-7)}}{2 \times 6}$ | M1   | <b>FT</b> <i>their</i> three term quadratic or for sketch of parabola with minimum point   |
|     |               |   |      | Alternative<br>If sketch of parabola with minimum point and $y = 1$ and no three term quadratic seen, allow <b>B3</b>  |
|     |               | x = 1.57  or  1.574<br>x = -0.741[01]                                     | B2   | <b>B1</b> for each   |

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| Que | stion        | Answer  | Mark | Part Marks   |
|-----|--------------|---|------|--|
| 14  | (a)          | Fully correct curve $ \begin{array}{c} 12  \mathbf{y} \\ 10 \\ 8 \\ 6 \\ 4 \\ 2 \\ -2 \\ -2 \\ -2 \\ -2 \\ -2 \\ -2 \\ -2 $ | 4    | <b>B1</b> for correct graph for $x < 0$ , minimum point<br>seen above <i>x</i> -axis<br><b>B1</b> for correct graph for $0 < x < 2$ , maximum<br>point seen higher than minimum point<br><b>B1</b> for minimum point seen below <i>x</i> -axis,<br>2 < x < 8<br>If 0 or 1 scored, <b>SC2</b> <u>instead</u> for 'correct curve'<br>except stationary point of inflexion instead of<br>LH minimum and maximum |
|     | (b)          | 0.729 or 0.7287<br>-10.3 or -10.26  | 2    | <b>B1</b> for each   |
|     | (c)          | (1.31 or 1.311 to 1.312, 1.73[0])   | 2    | <b>B1</b> for each co-ordinate   |
|     | ( <b>d</b> ) | -2.82, 0.364, 4.23, 5.76<br>or -2.824 to -2.823<br>0.3643 to 0.3644<br>4.228 to 4.229<br>5.758                              | 4    | <b>B1</b> for each<br>If 0 scored <b>SC2</b> for -2.8, 0.36, 4.2, 5.8<br>or <b>SC1</b> for three of these.   |