

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME				
CENTRE NUMBER		CANDIDATE NUMBER		

126258721

CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/51

Paper 5 (Core)

October/November 2014

1 hour

Candidates answer on the Question Paper.

Additional Materials: Graphics Calculator

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, glue or correction fluid.

You may use an HB pencil for any diagrams or graphs.

DO NOT WRITE IN ANY BARCODES.

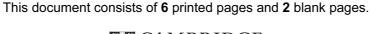
Answer all the questions.

You must show all relevant working to gain full marks for correct methods, including sketches.

In this paper you will also be assessed on your ability to provide full reasons and communicate your mathematics clearly and precisely.

At the end of the examination, fasten all your work securely together.

The total number of marks for this paper is 24.



Answer all the questions.

INVESTIGATION

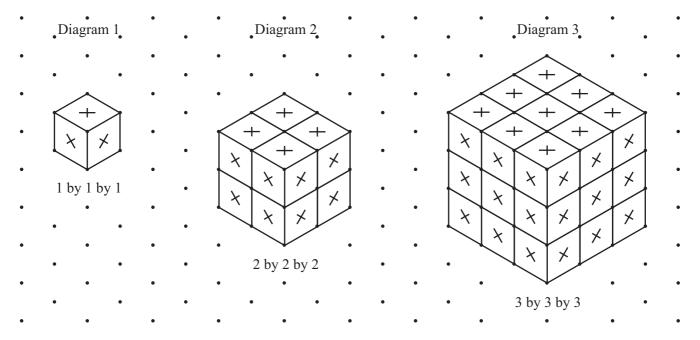
CUBES

Identical small cubes fit together to make larger cubes.

There are no gaps between these small cubes.

For each cube that is made, a cross is marked on each **outside** face of each small cube.

The diagram shows the first three cubes that can be made.



This investigation is about the number of crosses that can be marked on cubes.

Look at the 1 by 1 by 1 cube.

It is made from 1 small cube.

It has 6 crosses on it (3 crosses are on the faces not seen on the diagram).

1 Look at the 2 by 2 by 2 cube.

(a) How many small cubes is this cube made from?

.....

(b) Explain why there are only 3 crosses on each small cube.

(c) Find the total number of crosses on the 2 by 2 by 2 cube.

.....

2	Loo	ok at tl	he 3 b	y 3 by	y 3 cu	be.													
	(a)	How	man	y sma	ll cub	es is t	his cu	ibe m	ade fr	om?									
	(b)	How	man	y of tl	iese si	mall c	cubes	have :	3 cros	sses oi	n then	1?							
																		•••••	•••••
	(c)			12 sm small						them.									
		How	man	y sma	ll cub	es hav	ve onl	y 1 cr	oss o	n then	n?								
															••••	•••••		•••••	•••••
3	(a)	On t	he do	tty gri	d belo	ow, dr	aw a	4 by 4	4 by 4	cube	•								
		Marl	k a cro	oss on	the o	outside	e face	of ea	ch sm	all cu	be.								
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	(b)	The																	
		(i)	How	many	of th	ese sn	nall cı	ubes ł	nave 3	cross	ses on	them	?						
																•••••		•••••	•••••
		(ii)	How	many	of the	ese sn	nall c	ubes l	nave 2	cross	ses on	them	?						

4 Complete this table.

You may use the dotty grid on page 6 to help you.

Size of cube	Total number		Number of small cubes with												
Size of cube	of small cubes	0 crosses	1 cross	2 crosses	3 crosses										
2 by 2 by 2		0	0												
3 by 3 by 3		1		12											
4 by 4 by 4	64	8	24												
5 by 5 by 5		27	54		8										

5 (a) To work out the number of crosses on the 3 by 3 by 3 cube, complete the following.

1	small cube with	0	crosses gives	0	crosses
	small cubes with	1	cross gives	6	crosses
12	small cubes with	2	crosses gives		crosses
	small cubes with	3	crosses gives		crosses
			Total =		crosses

(b) The total number of crosses can also be worked out by the following method. Complete the following.

The number of crosses on one face of the 3 by 3 by 3	cube is
So the total number of crosses on all the 6 faces is	

(c) Find the total number of crosses on a 4 by 4 by 4 cube.

	٠.	٠.	٠.				٠	٠	•		٠			•	٠	•	•	٠	•	٠	٠	•	٠	•	•

6 (a) The number of small cubes with 0 crosses forms a sequence of cube numbers.

Size of cube	2 by 2 by 2	3 by 3 by 3	4 by 4 by 4	5 by 5 by 5	n by n by n
Number of small cubes with 0 crosses	0	1	8	27	

For an n by n by n cube, find an expression, in terms of n, for the number of small cubes with 0 crosses.

Write your answer in the table above.

(b)	The number of small cubes with 1 cross forms a sequence
	Find the <i>n</i> th term of this sequence.

.....

(c) The number of small cubes with 2 crosses forms a sequence. Find the *n*th term of this sequence.

.....

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