

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

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CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/41

Paper 4 (Extended)

October/November 2014

2 hours 15 minutes

Candidates answer on the Question Paper.

Additional Materials: Geometrical Instruments

Graphics Calculator

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, glue or correction fluid.

You may use an HB pencil for any diagrams or graphs.

DO **NOT** WRITE IN ANY BARCODES.

Answer all the questions.

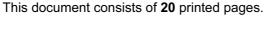
Unless instructed otherwise, give your answers exactly or correct to three significant figures as appropriate. Answers in degrees should be given to one decimal place.

For π , use your calculator value.

You must show all the relevant working to gain full marks and you will be given marks for correct methods, including sketches, even if your answer is incorrect.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 120.



Formula List

For the equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Curved surface area, A, of cylinder of radius r, height h.

$$A = 2\pi rh$$

Curved surface area, A, of cone of radius r, sloping edge l.

$$A = \pi r l$$

Curved surface area, A, of sphere of radius r.

$$A = 4\pi r^2$$

Volume, V, of pyramid, base area A, height h.

$$V = \frac{1}{3}Ah$$

Volume, V, of cylinder of radius r, height h.

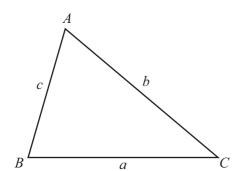
$$V = \pi r^2 h$$

Volume, V, of cone of radius r, height h.

$$V = \frac{1}{3}\pi r^2 h$$

Volume, V, of sphere of radius r.

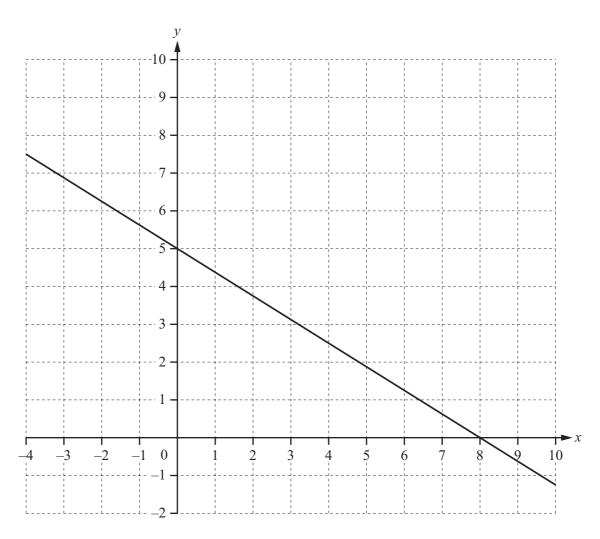
$$V = \frac{4}{3} \pi r^3$$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Area =
$$\frac{1}{2}bc \sin A$$



The diagram shows the graph of 5x + 8y = 40.

(a) On the grid, show accurately the region defined by these inequalities.

$$5x + 8y \ge 40 \qquad \qquad y \ge 2x + 3$$

[4]

(b) Find the minimum value of *y* in the region. Give your answer correct to 2 decimal places.

Answer(b) [3]

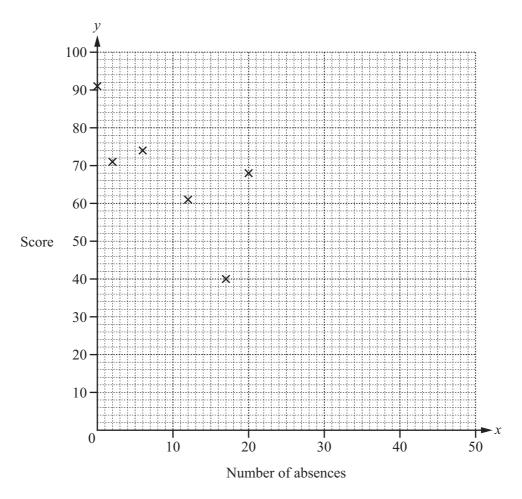
 $x \ge -2$

2 The table shows the scores (y) of 10 students in a mathematics test and their number of absences (x) from school.

Number of absences (x)	6	12	0	2	20	17	35	46	35	50
Score (y)	74	61	91	71	68	40	30	63	68	60

(a) Complete this scatter diagram.

The first six points have been plotted for you.



[2]

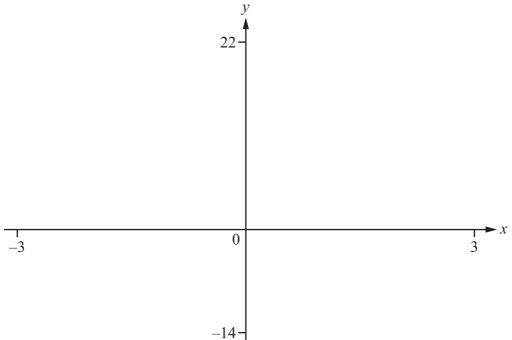
(b) What type of correlation is shown by the scatter diagram?

Answer(b) [1]

(c) Find the equation of the regression line. Write your answer in the form y = mx + c.

Answer(c) y = [2]

(d)	A s	tudent who had 26 absences missed the test.	
	(i)	Use your equation to estimate a score for that student.	
		Answer(d)(i)	[1]
	(ii)	The teacher does not have confidence in this estimate. Use your diagram to explain why.	
		Answer(d)(ii)	[1]
		y A	



(a) On the diagram, sketch the graph of $y = x^3 - 3x + 4$ for $-3 \le x \le 3$. [2]

(b) Describe fully the symmetry of the graph.

[3]

(c) Find the co-ordinates of the local maximum and local minimum.

Answer(c) Maximum (, ,)

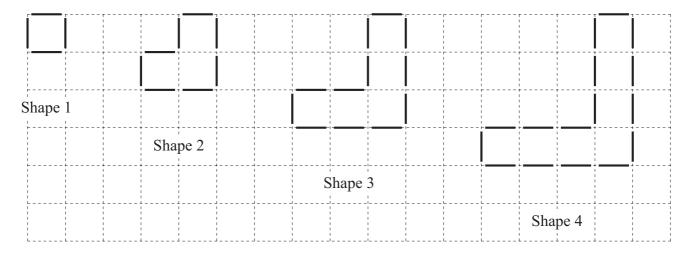
Minimum (_____ , ____) [2]

(d) Find the range of values of x for which y < 5.

Answer(d) [3]

4 (a) The shapes below form a sequence.

The shapes are made with 1 cm rods.



(i) Complete the table below.

Shape number	1	2	3	4	7	п
Number of rods	4	8	12	16		
Number of squares enclosed	1	3	5	7		

(ii) Find the number of squares enclosed by Shape 100.

Answer(a)(ii) [1]

[5]

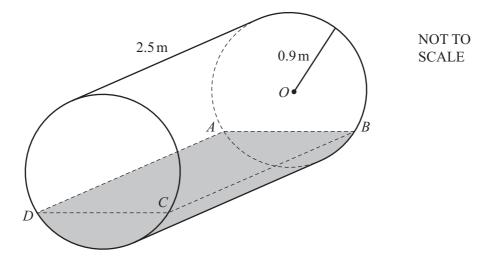
(b)	Here is another sequence of shapes made with 1 cm rods.	

-											 					т
Sh	ape 1	·	 	-			 				 	 			 	T
1				Shaj	pe 2											4
						 	 	S	hape	3						
			 					 					Sha	pe 4		

 [1]

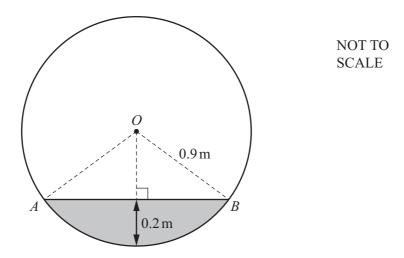
(ii) Find an expression, in terms of n, for the number of rods in Shape n.

5 The diagram below shows the cylindrical tank in which Dipak stores his heating oil.



The length of the tank is $2.5 \,\mathrm{m}$ and its radius is $0.9 \,\mathrm{m}$. Dipak measures the depth of the oil to be $0.2 \,\mathrm{m}$.

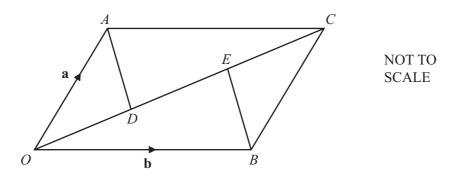
The diagram below shows the cross-section of the tank and the oil.



(a) Calculate the rectangular surface area of the oil, ABCD.

Answer(a) m^2 [4]

(b)	Calculate angle <i>AOB</i> and show that it rounds to 77.9° correct to 1 decimal place.		
				[3]
(c)	Find the number of extra litres of oil that Dipak needs to fill the tank.		
		Answer(c)	litres	[5]
		ZHSWEI (C)	111103	[ي]



The diagram shows a parallelogram, OACB. OC is a diagonal and OD = DE = EC.

 $\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OB} = \mathbf{b}$.

- (a) Find these vectors in terms of a and b. Write each answer in its simplest form.
 - (i) \overrightarrow{OC}

Answer(a)(i)	[1]

(ii) \overrightarrow{AD}

(b) Show that $\overrightarrow{EB} = \overrightarrow{AD}$.

[2]

[1]

(c) (i) What two conclusions can you make about AD and EB?

Answer(c)(i)

.....

(ii) What conclusion can you make about the quadrilateral AEBD?

Answer(c)(ii) [1]

7]	In a survey,	200 people	were asked	whether th	nev owned a	vehicle.
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130 owned a car (C), 30 owned a motorcycle (M) and 85 owned a bicycle (B).

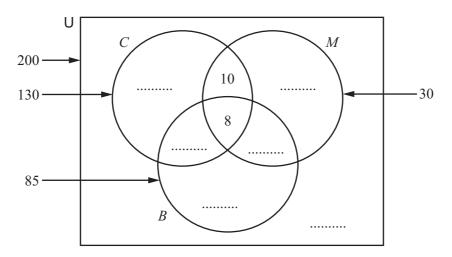
18 owned a car and a motorcycle.

17 owned a motorcycle and a bicycle.

60 owned a car and a bicycle.

8 owned a car and a motorcycle and a bicycle.

(a) Complete this Venn Diagram.



[3]

(b) Find the probability that a person, chosen at random from these 200 people,

(i) does not own any of the three vehicles,

Answer(b)(i)	Г17
Answer(D)(1)	111

(ii) is an element of the set $B \cap M \cap C'$.

(c) Two of the 200 people are chosen at random, without replacement.

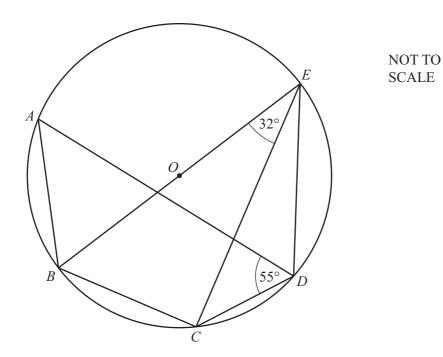
Calculate the probability that

(i) both own a motorcycle,

$$Answer(c)(i)$$
 [2]

(ii) one owns only a car and the other owns only a bicycle.

8 (a)



A, B, C, D and E are points on the circle centre O. BE is a diameter, angle $BEC = 32^{\circ}$ and angle $ADC = 55^{\circ}$.

Find

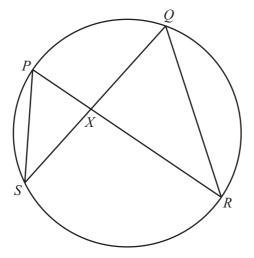
(i) angle EBC,

Answer(a)(i) Angle $EBC =$		[1]
----------------------------	--	-----

(ii) angle ABE.

$$Answer(a)(ii) Angle ABE =$$
 [2]

(b)



NOT TO SCALE

P, Q, R and S are points on a circle.
PR and QS intersect at X.
PS = 8 cm $QR = 12 cm$ and $PV = 5 cm$

	(i)	Explain why	z trianala	DYC ic	cimilar t	o triangle	OYP
- (1)	Explain will	y uriangie	PASIS	Sillillar u	o mangie	OAR.

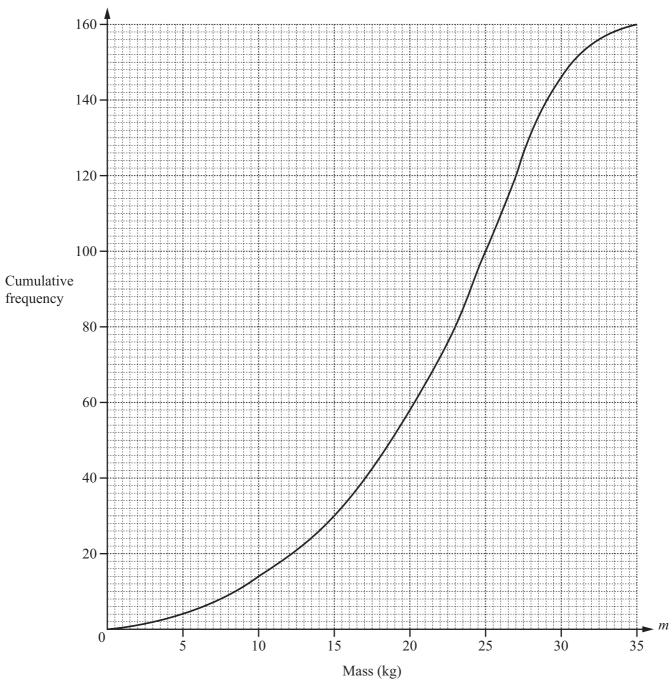
Answer(b)(i)	
	[2]

(ii) Calculate the length of QX.

Answer(b)(ii) cm	[2]
------------------	-----

(iii) Find the value of $\frac{\text{Area of triangle } PXS}{\text{Area of triangle } QXR}$.

9 A transport company records the masses, $m \log n$, of 160 parcels it delivers. The cumulative frequency curve shows this information.



(a) (i) Find the median.

Answer(a)(i) kg [1]

(ii) Find the lower quartile.

Answer(a)(ii) kg [1]

(iii) Find the interquartile range.

Answer(a)(iii) kg [1]

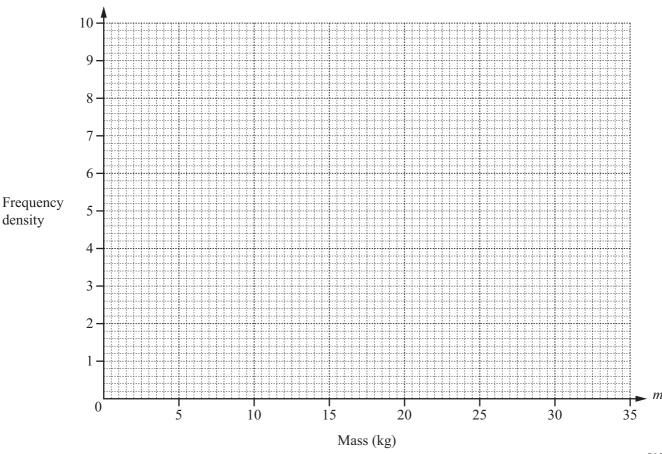
(b) Use the cumulative frequency curve to complete the frequency table.

Mass (m kg)	$0 < m \le 10$	$10 < m \le 15$	$15 < m \le 20$	$20 < m \le 25$	$25 < m \le 35$
Frequency	14		28		

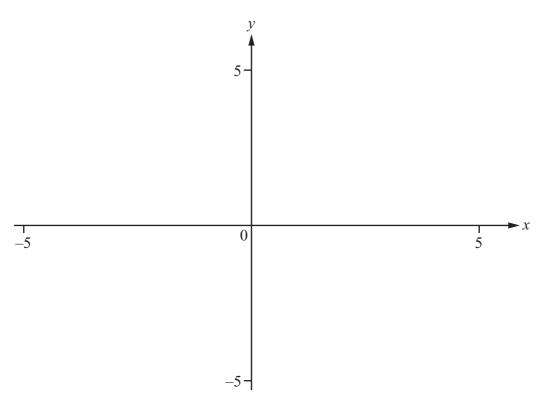
[3]

(c) On the grid below, use the results from part (b) to draw a histogram.

density



[3]



(a) $f(x) = 10^x - 3$.

G)	On the diagram, sket	ch the graph of	y = f(x)	ra	7
(1)	On the diagram, sket	ch the graph of	y = I(x).	4	41

(ii) Write down the equation of the asymptote of f(x).

(b) $g(x) = \tan 30x^{\circ}$.

(i) On the same diagram, sketch the graph of
$$y = g(x)$$
. [3]

(ii) Write down the equations of the vertical asymptotes of g(x) for values of x between -5 and 5.

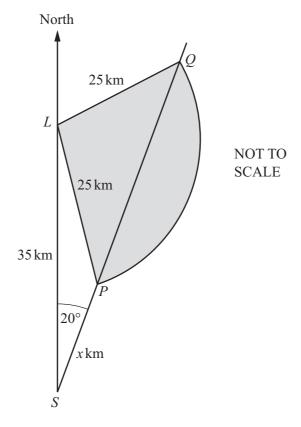
$$Answer(b)(ii)$$
 [2]

(c) Solve the equation f(x) = g(x) for values of x between -5 and 5.

$$Answer(c) \qquad [2]$$

11 Janine and Gitte work for the same company.

(a)	In 2010, the ratio Janine's salary: Gitte's salary was 5:4. The total of their salaries was \$95400.			
	Find each of their salaries in 2010.			
	Answer(a) Janine \$			
	Gitte \$ [2	.]		
(b)	Each of their salaries was a 6% increase on their 2009 salaries.			
	(i) Write down the ratio of their salaries in 2009.			
	Answer(b)(i) : [1]		
	(ii) Find the total of their salaries in 2009.			
	Answer(b)(ii) [3]		
(c)	In 2011, Janine and Gitte each received an increase of the same amount of money. In 2011, the ratio Janine's salary: Gitte's salary was 11:9.			
	Find the increase they each received.			
	Answer(c) [3]		
(d)	In 2012 Janine's friend, Alain, received a salary increase of 8%. In 2013, his salary was reduced by 8%.			
	Find the percentage change in Alain's salary over the two years. Say whether it is an increase or decrease.			
	Answer(d) by % [3	1		
	70 [3	J		



A ship sails from S on a bearing of 020° . There is a lighthouse at L, 35 km due north of S. The light from the lighthouse has a range of 25 km. SP = x km.

(a) Use the cosine rule to show that $x^2 - kx + 600 = 0$, where k = 65.78 correct to 2 decimal places.

Answer(b) $x =$	(b)	(i)	Solve the equation	$x^2 - 65.78x + 60$	00 = 0, giving	your answers	correct to 2	decimal pla	ces.	
(ii) Write down the distance SQ. Answer(b)(ii) km [1] (c) The ship is sailing at 30 km/h. Use your answers to part (b) to find the length of time the light is visible from the ship. Give your answer in hours and minutes correct to the nearest minute.										
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(c) The ship is sailing at 30 km/h. Use your answers to part (b) to find the length of time the light is visible from the ship. Give your answer in hours and minutes correct to the nearest minute.		(;;)	White deven the dist	tomas SO						
(c) The ship is sailing at 30 km/h. Use your answers to part (b) to find the length of time the light is visible from the ship. Give your answer in hours and minutes correct to the nearest minute.		(11)	write down the dist	ance SQ.						
Use your answers to part (b) to find the length of time the light is visible from the ship. Give your answer in hours and minutes correct to the nearest minute.					Answer(b)(i	i)			km	[1]
Use your answers to part (b) to find the length of time the light is visible from the ship. Give your answer in hours and minutes correct to the nearest minute.	(c)	The	ship is sailing at 30	km/h.						
	()	Use	your answers to par	t (b) to find the			ible from t	he ship.		
<i>Answer(c)</i> h min [3]		Giv	e your answer in hou	irs and minutes c	orrect to the r	nearest minute.				
<i>Answer(c)</i> h min [3]										
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					Answer(c)		h		min	[3]

13	(a)	f(x) = 3x - 2 Find h(g(0)).	g(x) = x + 3	$h(x) = 2x^2 + 7x + 3$	
	(b)	Find $f(g(x))$, writing your ans			[1]
	(c)	Find $f^{-1}(x)$.	Answer(b)		[2]
			Answer(c)	,	[2]

(d) Simplify

Answer(d) [3]

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