Cambridge Assessment International Education
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS **0606/21**

Paper 2 **October/November 2019**

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2019 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1: Marks must be awarded in line with: • the specific content of the mark scheme or the generic level descriptors for the question • the specific skills defined in the mark scheme or in the generic level descriptors for the question • the standard of response required by a candidate as exemplified by the standardisation scripts.
GENERIC MARKING PRINCIPLE 2: Marks awarded are always **whole marks** (not half marks, or other fractions).
GENERIC MARKING PRINCIPLE 3: Marks must be awarded **positively**: • marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate • marks are awarded when candidates clearly demonstrate what they know and can do • marks are not deducted for errors • marks are not deducted for omissions • answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.
GENERIC MARKING PRINCIPLE 4: Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.
GENERIC MARKING PRINCIPLE 5: Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).
GENERIC MARKING PRINCIPLE 6: Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method marks, awarded for a valid method applied to the problem.

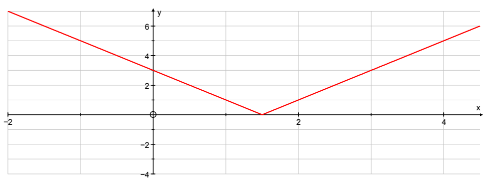
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt answers which round to
cao correct answer only
dep dependent
FT follow through after error
isw ignore subsequent working
nfww not from wrong working
oe or equivalent
rot rounded or truncated
SC Special Case
soi seen or implied

Question	Answer	Marks	Partial Marks
1(i)		**B2**	**B1** shape **B1** Correct intersection with axes.
1(ii)	$7 = 2x - 3 \rightarrow x = 5$	**B1**	
	Uses $7 = 3 - 2x$ oe	**M1**	
	$x = -2$	**A1**	
2	$p = 2$ $q = 4$ $r = 3$	**B3**	**B1** for each

Question	Answer	Marks	Partial Marks
3(a)	obtain $e^{5x-3} = 3$	M1	**OR** Take logs → $2x + 1 = \ln 3 + 4 - 3x$
	take logs correctly → $5x - 3 = \ln 3$	M1	**OR** Collect like terms → $5x = 3 + \ln 3$
	$x = \dfrac{3+\ln 3}{5}$ or $x = 0.820$	A1	
3(b)`	Use of laws of logs → $\lg(y-6)(y+15) = 2$	M1	
	Uses $10^2 = 100$ → $[(y-6)(y+15)] = 100$	B1	
	Obtain correct quadratic → $y^2 + 9y - 190 = 0$	A1	
	Solve a three term quadratic	M1	
	$y = 10$ only	A1	
4	Eliminate x or y	M1	
	$x = \dfrac{7+5\sqrt{2}}{3+2\sqrt{2}}$ or $y = \dfrac{1}{3+2\sqrt{2}}$	A1	
	Multiply numerator and denominator by $3-2\sqrt{2}$	M1	
	$x = 1+\sqrt{2}$	A1	
	$y = 3-2\sqrt{2}$	A1	
5(i)	Differentiate	M1	Obtain $2\cos 2t$ or $-2\sin 2t$
	$v = 6\cos 2t - 8\sin 2t$	A1	
	$a = -12\sin 2t - 16\cos 2t$	A1	
5(ii)	Equate v to 0 and attempt to solve	M1	
	$\tan 2t = 0.75$	A1	or $\sin 2t = 0.6$ or $\cos 2t = 0.8$
	$t = 0.32(2)$	A1	Must be in radians
5(iii)	Insert value of t into expression for a	M1	Radians or degrees
	$a = -20$	A1	Must have used radians

Question	Answer	Marks	Partial Marks
6	Eliminate y	**M1**	
	$x^2 - x - 5 = 0$	**A1**	
	Use formula	**M1**	
	$x = \frac{1 \pm \sqrt{21}}{2}$	**A1**	
	$y = \frac{21 \pm \sqrt{21}}{2}$	**A1**	
	Find mid-point	**M1**	$(0.5, 10.5)$
	Show that mid-point lies on $x + y = 11$	**A1**	
7(a)(i)	$\mathrm{f}(0.5) = 0.5 + 4.5 - 5 = 0$	**B1**	
7(a)(ii)	Factorise to obtain $2x^2$ and 5	**M1**	
	$(2x-1)(2x^2 + x + 5)$	**A1**	
7(b)(i)	Replace $\tan x$ by $\frac{\sin x}{\cos x}$ and $\sec x$ by $\frac{1}{\cos x}$	**M1**	$13\frac{\sin x}{\cos^2 x} - 4\sin x - \frac{5}{\cos^2 x} = 0$
	Uses $\cos^2 x = 1 - \sin^2 x$	**M1**	$13\sin x - 4\sin x(1 - \sin^2 x) - 5 = 0$
	$4\sin^3 x + 9\sin x - 5 = 0$	**A1**	Completed correctly
7(b)(ii)	$2\sin^2 x + \sin x + 5 = 0$ no real roots	**B1**	Suitable statement seen
	$2\sin x - 1 = 0$	**M1**	Attempt to solve
	$x = \frac{\pi}{6}$	**A1**	
	$x = \frac{5\pi}{6}$	**A1**	
8(i)	$-2e^{-2x}$ seen	**B1**	
	Product rule	**M1**	Clear attempt
	$e^{-2x}(1 - 2x)$	**A1**	

Question	Answer	Marks	Partial Marks
8(ii)	Set $\frac{dy}{dx}=0$ and attempt to solve	**M1**	Must have two terms
	$\left(\frac{1}{2}, \frac{1}{2e}\right)$	**A1**	
8(iii)	Attempt to find $\frac{dy}{dx}$ at $x=1$	**M1**	
	$y-\frac{1}{e^2}=\frac{-1}{e^2}(x-1)$ or $y=-\frac{1}{e^2}x+\frac{2}{e^2}$	**A1**	
8(iv)	Integrate **part(i)** $xe^{-2x}=\int\left(-2xe^{-2x}+e^{-2x}\right)dx$	**M1**	
	Integrate e^{-2x} and make $\int xe^{-2x}dx$ the subject	**M1**	
	$\frac{-xe^{-2x}}{2}-\frac{e^{-2x}}{4}+c$	**A1**	
9(i)	$\frac{1}{3}$	**B1**	
	$\times\begin{pmatrix}-3 & -2\\ 9 & 5\end{pmatrix}$	**B1**	
9 (ii)	$\mathbf{B}^2=\begin{pmatrix}10 & 7\\ 42 & 31\end{pmatrix}$	**B2**	Minus one each error
9(iii)	$\mathbf{C}=\mathbf{B}^2-\mathbf{BA}$	**M1**	
	$\mathbf{BA}=\begin{pmatrix}1 & 1\\ -15 & -3\end{pmatrix}$	**A1**	
	$\mathbf{C}=\begin{pmatrix}9 & 6\\ 57 & 34\end{pmatrix}$	**A1**	
9(iv)	$\mathbf{D}=\mathbf{B}^2\mathbf{A}^{-1}$	**M1**	
	$\mathbf{D}=\frac{1}{3}\begin{pmatrix}33 & 15\\ 153 & 71\end{pmatrix}$	**A2**	Minus one each error
10(i)	$81+108x+54x^2+12x^3+x^4$	**B3**	**B1** for coefficients **B1** for powers **B1** for all Correct

Question	Answer	Marks	Partial Marks
10(ii)	Identify and select two terms in x and equate to zero	**M1**	$81 - 54p = 0$
	$p = 1.5$	**A1**	
10(iii)	Constant term = $-108p = -162$	**A1**	**FT** using *their p*
10(iv)	Correctly identify two terms in x^2	**M1**	x^2 term = $108 - 12p$
	$108 - 18 = 90$	**A1**	
11(i)	Uses correct triangle with v_w opposite 10° Sides of 300 and 280 include 10°	**M1**	
	Use cosine rule	**M1**	${v_w}^2 = 300^2 + 280^2 - 2 \times 300 \times 280 \cos 10$
	$v_w = 54.3$	**A1**	
11(ii)	Use sine rule	**M1**	$\frac{280}{\sin\alpha} = \frac{54.3}{\sin 10°}$
	$\alpha = 63°$ or $64°$	**A1**	
	Bearing 117° or 116°	**A1**	