CAMBRIDGE INTERNATIONAL EXAMINATIONS

International General Certificate of Secondary Education

MARK SCHEME for the May/June 2014 series

0606 ADDITIONAL MATHEMATICS

0606/12 Paper 1, maximum raw mark 80

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Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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1	$\frac{\cos^2 A + (1 + \sin A)^2}{(1 + \sin A)\cos A}$ $\frac{\cos^2 A + 1 + 2\sin A + \sin^2 A}{(1 + \sin A)\cos A}$ $= \frac{2(1 + \sin A)}{(1 + \sin A)\cos A}$	M1 M1 DM1	M1 for obtaining a single fraction, correctly M1 for expansion of $(1 + \sin A)^2$ and use of identity DM1 for factorisation and cancelling of $(1 + \sin A)$ factor
	$= \frac{2}{\cos A} = 2 \sec A$	A1	A1 for use of $\frac{1}{\cos A} = \sec A$ and final answer
	Alternative: $ \frac{\cos A (1 - \sin A)}{(1 + \sin A)(1 - \sin A)} + \frac{1 + \sin A}{\cos A} $ $ = \frac{\cos A (1 - \sin A)}{1 - \sin^2 A} + \frac{1 + \sin A}{\cos A} $	M1	M1 for multiplying first term by $\frac{1-\sin A}{1-\sin A}$
	$= \frac{\cos A \left(1 - \sin A\right)}{\cos^2 A} + \frac{1 + \sin A}{\cos A}$	M1	M1 for expansion of $(1-\sin A)(1+\sin A)$ and use of
	$= \frac{1 - \sin A}{\cos A} + \frac{1 + \sin A}{\cos A}$	M1	identity M1 for simplification of the 2 terms
	$= \frac{2}{\cos A} = 2 \sec A$	A1	A1 for use of $\frac{1}{\cos A} = \sec A$ and final answer
2 (a) (i)		B1	
(i)		B1	
(b) (i)	6	B1	
(ii)	5	B1	
(iii)	9	B1	

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3 (i) (ii)	Maximum point occurs when $y = \frac{25}{8}$	B1 B1 B1	 B1 for shape B1 for y = 2 (must have a graph) B1 for x = -0.5 and 2 (must have a graph) M1 for obtaining the value of y at the maximum point, by either completing the square, differentiation, use of discriminant or symmetry.
	so $k > \frac{25}{8}$	A1	Must have the correct sign for A1 Ignore any upper limits
4	$\int_0^a \sin 3x dx = \frac{1}{3} dx = \frac{1}{3}$ $\left[-\frac{2}{3} \cos 3x \right]_0^a = \frac{1}{3}$ $\left(-\frac{2}{3} \cos 3a \right) - \left(-\frac{2}{3} \right) = \frac{1}{3}$ $\cos 3a = 0.5$ $3a = \frac{\pi}{3}, \ a = \frac{\pi}{9}$	M1 A1 M1 A1	B1 for $k \cos 3x$ only, B1 for $-\frac{2}{3}\cos 3x$ only M1 for correct substitution of the correct limits into their result A1 for correct equation M1 for correct method of solution of equation of the form $\cos ma = k$ A1 allow 0.349, must be a radian answer
5 (i)	$2^{5x} \times 2^{2y} = 2^{-3}$ leads to $5x + 2y = -3$	B1, B1 DB1	B1 for 2 ^{2y} , B1 for 2 ⁻³ , B1 for dealing with indices correctly to obtain given answer
(ii)	$7^x \times 49^{2y} = 1$ can be written as $x + 4y = 0$	B1 B1	B1 for either 7^{4y} or 7^0 seen B1 for $x + 4y = 0$
	Solving $5x + 2y = -3$ and $x + 4y = 0$ leads to $x = -\frac{2}{3}, y = \frac{1}{6}$	M1	M1 for solution of their simultaneous equations, must both be linearA1 for both, allow equivalent fractions only

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6	(a)	YX and ZY	B1,B1	B1 for each, must be in correct order,
	(b)	$\mathbf{B} = \mathbf{A}^{-1} \begin{pmatrix} 3 & 9 \\ -6 & -3 \end{pmatrix},$	M1	M1 for pre-multiplication by A ⁻¹
		$= -\frac{1}{3} \begin{pmatrix} 1 & 2 \\ 4 & 5 \end{pmatrix} \begin{pmatrix} 3 & 9 \\ -6 & -3 \end{pmatrix}$	B1,B1	B1 for $-\frac{1}{3}$, B1 for $\begin{pmatrix} 1 & 2 \\ 4 & 5 \end{pmatrix}$
		$= -\frac{1}{3} \begin{pmatrix} -9 & 3 \\ -18 & 21 \end{pmatrix} \text{ or } \begin{pmatrix} 3 & -1 \\ 6 & -7 \end{pmatrix}$	DM1	DM1 for attempt at matrix multiplication A1 allow in either form
		Alternative method:		
		$ \begin{pmatrix} 5 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 3 & 9 \\ -6 & -3 \end{pmatrix} $	M1	M1 for a complete method to obtain 4 equations
		Leads to $5a - 2c = 3$, $5b - 2d = 9$ -4a + c = -6, $-4b + d = -3$	A2,1,0	-1 for each incorrect equation
		Solutions give matrix	M1	M1 for solution to find 4 unknowns
		$-\frac{1}{3} \begin{pmatrix} -9 & 3 \\ -18 & 21 \end{pmatrix} \text{ or } \begin{pmatrix} 3 & -1 \\ 6 & -7 \end{pmatrix}$	A1	A1 for a correct, final matrix

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7	(i)	$\sin \frac{\theta}{2} = \frac{6}{8}, \frac{\theta}{2} = 0.8481 \text{ or better}$ or $12^2 = 8^2 + 8^2 - 128 \cos \theta$	M1	M1 for a complete method to find either θ or $\frac{\theta}{2}$
		$\theta = 1.6961$ or better	A1	Answer given.
		or using areas $\frac{1}{2} \times 12 \times 2\sqrt{7} = \frac{1}{2} 8^2 \sin \theta \text{ oe}$		
		$\sin \theta = 0.9922$, $\theta = 1.4455$ or 1.6961	M1	M1 for using the area of the
			A1	triangle in 2 different forms A1 for choosing the correct angle.
	(ii)	Arc length = $(2\pi - 1.696) \times 8$	M1	M1 for correct attempt at a minor or major arc length
		(36.697 or 36.7)	A1	A1 for correct major arc length, allow unsimplified
		Perimeter = $12 + (2\pi - 1.696) \times 8$ = 48.7	A1	A1 for 48.7 or better
	(iii)	Area = $\frac{8^2}{2} (2\pi - 1.696) + \frac{8^2}{2} \sin 1.696$	M1,M1	M1 for correct attempt to find area of major sector
		=178.5, 178.6, awrt179	A1	M1 for correct attempt to find area of triangle, using any method
		Alternative:		
		Area = $\pi 8^2 - \left(\frac{1}{2}8^2(1.696) - \frac{8^2}{2}\sin 1.696\right)$		M1 for attempt at area of circle – area of minor sector M1 for area of triangle

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8 (a) (i)	720	B1	
(ii)	240	B1	
(iii)	Starts with either a 2 or a 4: 48 ways	B1	allow unevaluated
	Does not start with either a 2 or a 4: 96 ways (i.e. starts with 1 or 5)	B1	allow unevaluated
	Total = 144	B1	must be evaluated
	Alternative 1:		
	Ends with a 2, starts with a 1,4 or 5:72 ways Ends with a 4, starts with a 1,2 or 5:72 ways Total =144	B1 B1 B1	
	Alternative 2:		
	$240 - (2 \times 2 \times^{4} P_{3}) \text{ or } (4 \times^{4} P_{3} \times 2) - (2^{4} P_{3})$ $= 144$	B2 B1	B2 for correct expression seen, allow <i>P</i> notation
	Alternative 3:		
	${}^{3}P_{1} \times {}^{4}P_{3} \times {}^{2}P_{1}$ or $3 \times 4 \times 2$ = 144	B2 B1	Allow <i>P</i> notation here, for B2
(b)	With twins: ${}^{16}C_4$ (=1820)	B1	
	Without twins: ${}^{16}C_6 \ (= 8008)$	B1	
	Total: 9828	B1	
	Alternative:		
	$^{18}C_6 - (2 \times^{16} C_5)$ = 9828	B1,B1 B1	B1 for ${}^{18}C_6$ –, B1 for $2 \times {}^{16}C_5$

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9	(i)	$h = \frac{4000}{\pi r^2} \text{ or } \pi r^2 h = 4000$ $A = 2\pi r h + 2\pi r^2$	B1	
		$A = 2\pi r \frac{4000}{\pi r^2} + 2\pi r^2$	M1 A1	M1 for substitution of h or πrh into their equation for A A1 Answer given
	(ii)	$\frac{\mathrm{d}A}{\mathrm{d}r} = -\frac{8000}{r^2} + 4\pi r$	B1, B1	B1 for each term correct
		When $\frac{dA}{dr} = 0$, $r^3 = \frac{8000}{4\pi}$	M1	M1 for equating to zero and attempt to find r^3
		leading to $A = 1395, 1390$	M1	M1 for substitution of their r to obtain A .
			A1	A1 for 1390 or awrt 1395
		$\frac{d^2 A}{dr^2} = \frac{16000}{r^3} + 4\pi,$ which, is positive so a minimum.	√ B1	√B1 for a complete correct method and conclusion.

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10 (i)	Velocity = $26 \times \frac{1}{13} (5\mathbf{i} + 12\mathbf{j})$ = $10\mathbf{i} + 24\mathbf{j}$	M1 A1	M1 for $\frac{1}{13}$ (5 i + 12 j)
	Alternative 1: $ 10\mathbf{i} + 24\mathbf{j} = \sqrt{10^2 + 24^2}$ = 26	M1	M1 for working from given answer to obtain the given speed
	Showing that one vector is a multiple of the other, hence same direction	A1	A1 for a completely correct method
	Alternative 2: $\sqrt{5^2 + 12^2} = 13$, $13k = 26$, so $k = 2$ Velocity = $2(5\mathbf{i} + 12\mathbf{j})$,	M1	M1 for attempt to obtain the 'multiple' and apply to the direction vector
	Velocity = $10\mathbf{i} + 24\mathbf{j}$	A1	A1 for a completely correct method
	Alternative 3: Use of trig: $\tan \alpha = \frac{12}{5}$, $\alpha = 67.4^{\circ}$		
	Velocity $26\cos 67.4^{\circ} \mathbf{i} + 26\sin 67.4 \mathbf{j}$	M1	M1 for reaching this stage
	Velocity = 10i + 24j	A1	A1 for a completely correct method
(ii)	Position vector = $4(10\mathbf{i} + 24\mathbf{j})$ or $40\mathbf{i} + 96\mathbf{j}$	B1	Allow either form for B1
(iii)	(40i + 96j) + (10i + 24j)t oe	M1	M1 for their (ii) + $(10\mathbf{i} + 24\mathbf{j})t$ or
		A1	$(10\mathbf{i} + 24\mathbf{j}) \times (t+4)$ A1 correct answer only
(iv)	(120i + 81j) + (-22i + 30j)t oe	B1	
(v)	40 + 10t = 120 - 22t or $96 + 24t = 81 + 30t$	M1	M1 for equating like vectors
	t = 2.5 or 18:30	A1	A1 Allow for $t = 2.5$
	Position vector $= 65\mathbf{i} + 156\mathbf{j}$	DM1	DM1 for use of t to obtain position vector
		A1	A1 cao

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11 (a)	$\tan x(\tan x + 5) = 0$ $\tan x = 0$, $x = 0^{\circ}, 180^{\circ}$ $\tan x = -5$, $x = 101.3^{\circ}$	B1,B1 B1	B1 for each , must be from correct work
(b)	$2(1-\sin^2 y) - \sin y - 1 = 0$ $2\sin^2 y + \sin y - 1 = 0$ $(2\sin y - 1)(\sin y + 1) = 0$	M1	M1 for use of correct identity and attempt to solve resulting 3 term quadratic equation.
	$\sin y = \frac{1}{2}, y = 30^{\circ}, 150^{\circ}$	A1,A1	
	$\sin y = -1, y = 270^{\circ}$	A1	
(c)	$\cos\left(2z - \frac{\pi}{6}\right) = \frac{1}{2}$ $\left(2z - \frac{\pi}{6}\right) = \frac{\pi}{3}$	M1	M1 for dealing with sec correctly and obtaining $\frac{\pi}{3}$ or 1.05
	$\left(2z - \frac{\pi}{6}\right) = \frac{\pi}{3}$	A.1	
	$z = \frac{\pi}{4} \text{ or } 0.785 \text{ or better}$	A1	
	$\left(2z - \frac{\pi}{6}\right) = \frac{5\pi}{3}$	M1	M1 for obtaining a second equation $\left(2z - \frac{\pi}{6}\right) = 2\pi - their \frac{\pi}{3} \text{ oe}$
	$z = \frac{11\pi}{12}$ or 2.88 or better	A1	