

Cambridge International Examinations Cambridge International General Certificate of Secondary Education

CANDIDATE NAME						
CENTRE NUMBER		CANDIDATE NUMBER				
MATHEMATICS		0580/42				
Paper 4 (Extended)		February/March 2018				
		2 hours 30 minutes				
Candidates answer	on the Question Paper.					
Additional Materials	: Electronic calculator Tracing paper (optional)	Geometrical instruments				

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.

This document consists of **15** printed pages and **1** blank page.



- 1 (a) A shop sells dress fabric for \$2.97 per metre.
 - (i) A customer buys 9 metres of this fabric.

Calculate the change he receives from \$50.

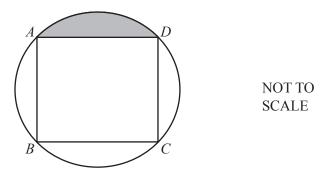
Calculate the difference in price when the exchange rate is 1 rupee = \$0.0153.

Give your answer in rupees.

..... rupees [2]

(c) The dressmaker measures a length of fabric as 600 m, correct to the nearest 5 metres. He cuts this into dress lengths of 9 m, correct to the nearest metre.

Calculate the largest number of complete dress lengths he could cut.



The vertices of a square ABCD lie on the circumference of a circle, radius 8 cm.

(a) Calculate the area of the square.

..... cm² [2]

(b) (i) Calculate the area of the shaded segment.

..... cm² [3]

(ii) Calculate the perimeter of the shaded segment.

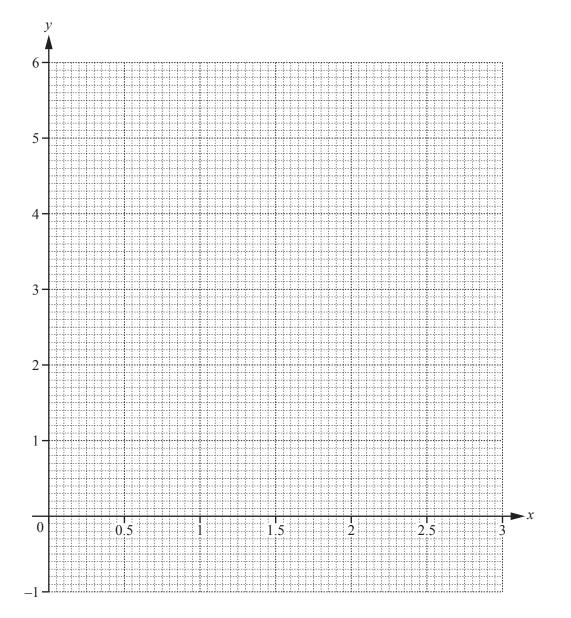
..... cm [4]

3 The table shows some values for $y = 2x + \frac{1}{x} - 3$ for $0.125 \le x \le 3$.

x	0.125	0.25	0.375	0.5	0.75	1	1.5	2	2.5	3
у	5.25	1.5	0.42			0	0.67	1.5		3.33

(a) Complete the table.

(b) On the grid, draw the graph of $y = 2x + \frac{1}{x} - 3$ for $0.125 \le x \le 3$.



[3]

[4]

(c) Use your graph to solve $2x + \frac{1}{x} - 3 \ge 2$.

.....[3]

(d) The equation $\frac{1}{x} = 7 - 3x$ can be solved using your graph in **part** (b) and a straight line.

(i) Write down the equation of this straight line.

.....[2]

(ii) Draw this straight line and solve the equation $\frac{1}{x} = 7 - 3x$.

 $x = \dots$ [3]

4 (a) Make t the subject of the formula $s = k - t^2$.

 $t = \dots [2]$

(b) (i) Factorise $x^2 - 25$.

(ii) Simplify $\frac{x^2 - 25}{x^2 - 2x - 35}$.

.....[3]

.....[1]

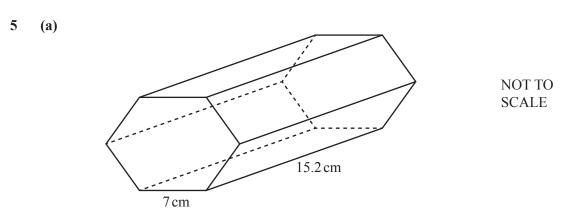
(c) Write as a single fraction in its simplest form.

$$\frac{x-8}{x} + \frac{3x}{x+1}$$

.....[3]

(d) Find the integer values of *n* that satisfy the inequality.

 $18 - 2n < 6n \leq 30 + n$



7

The diagram shows a solid prism with length 15.2 cm. The cross-section of this prism is a **regular** hexagon with side 7 cm.

(i) Calculate the volume of the prism.

..... cm³ [5]

(ii) Calculate the total surface area of the prism.

..... cm² [3]

(b) Another solid metal prism with volume 500 cm³ is melted and made into 6 identical spheres.Calculate the radius of each sphere.

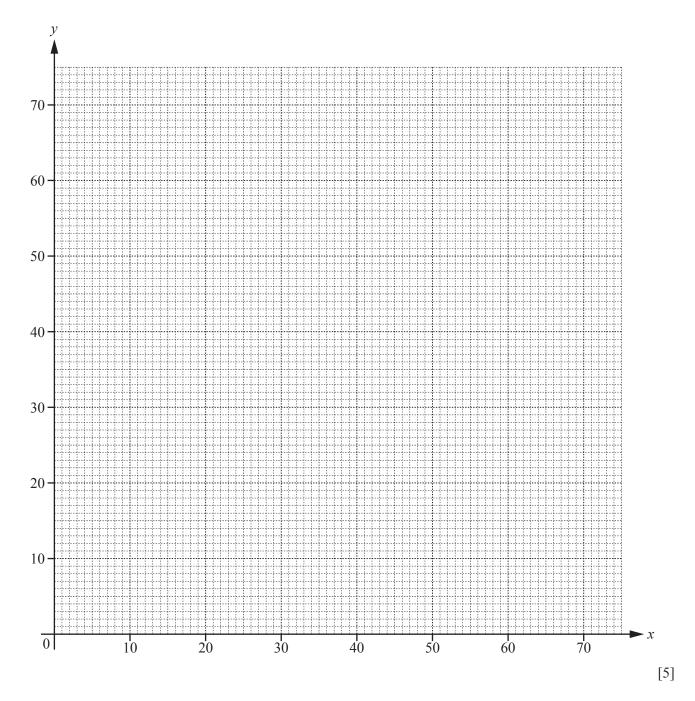
[The volume, V, of a sphere with radius r is $V = \frac{4}{3}\pi r^3$.]

6 Klaus buys *x* silver balloons and *y* gold balloons for a party.

He buys

- more gold balloons than silver balloons
- at least 15 silver balloons
- less than 50 gold balloons
- a total of no more than 70 balloons.
- (a) Write down four inequalities, in terms of x and/or y, to show this information.

......[4]



(b) On the grid, show the information from **part (a)** by drawing four straight lines and shading the unwanted regions.

(c) Silver balloons cost \$2 and gold balloons cost \$3.

Calculate the most that Klaus could spend.

Time (<i>m</i> minutes)	$0 < m \leq 10$	$10 < m \leq 40$	$40 < m \leqslant 60$	$60 < m \leqslant 90$	$90 < m \le 100$	$100 < m \le 120$
Frequency	3	39	43	55	11	9

7 The frequency table shows information about the time, *m* minutes, that each of 160 people spend in a library.

(a) (i) Find the probability that one of these people, chosen at random, spends more than 100 minutes in the library.

(ii) Calculate an estimate of the mean time spent in the library.

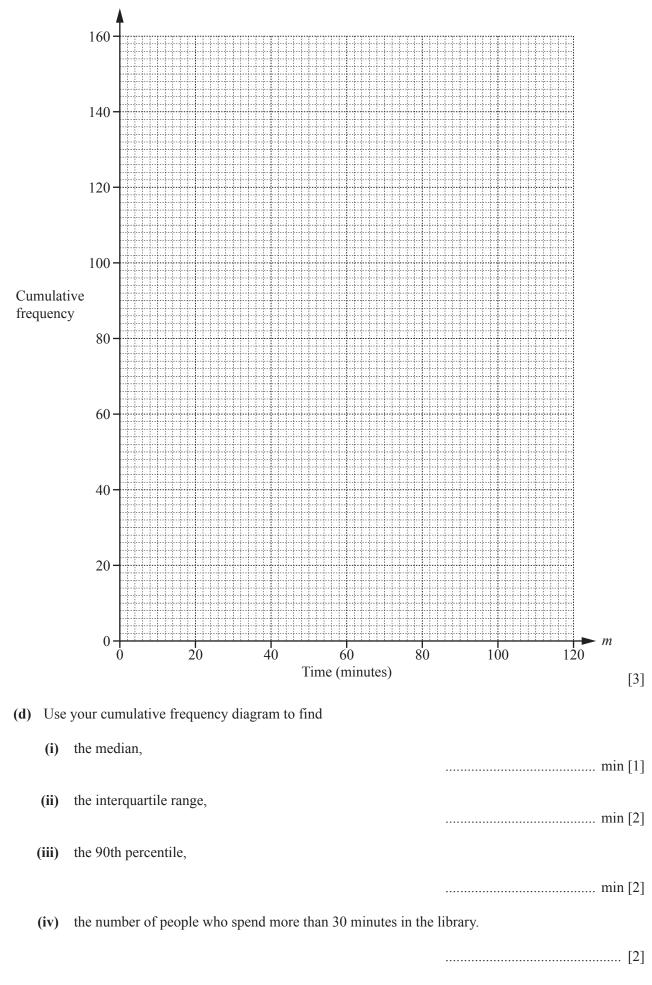
..... min [4]

(b) Complete the cumulative frequency table below.

Time (<i>m</i> minutes)	<i>m</i> ≤ 10	$m \leq 40$	$m \leq 60$	<i>m</i> ≤ 90	<i>m</i> ≤ 100	<i>m</i> ≤ 120
Cumulative frequency	3	42				

[2]

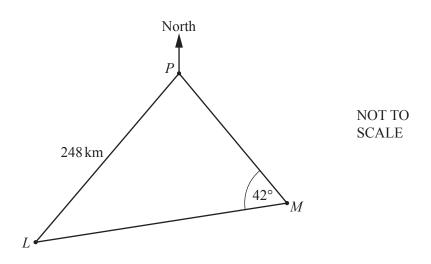
(c) On the grid opposite, draw the cumulative frequency diagram.



0580/42/F/M/18

[Turn over





The diagram shows two ports, *L* and *P*, and a buoy, *M*. The bearing of *L* from *P* is 201° and LP = 248 km. The bearing of *M* from *P* is 127°. Angle *PML* = 42°.

(a) Use the sine rule to calculate *LM*.

LM = km [4]

(b) A ship sails directly from L to P.

(i) Calculate the shortest distance from *M* to *LP*.

..... km [3]

(ii) The ship leaves L at 2045 and travels at a speed of 40 km/h.

Calculate the time the next day that the ship arrives at *P*.

9 (a) Find the magnitude of the vector $\begin{pmatrix} -1 \\ 7 \end{pmatrix}$.

.....[2]

(b) The determinant of the matrix
$$\begin{pmatrix} 6 & 2m \\ 5 & m \end{pmatrix}$$
 is 24.
Find the value of *m*.

 $m = \dots [2]$

(c)
$$\mathbf{L} = \begin{pmatrix} 2 & 5 \\ 3 & 9 \end{pmatrix}$$
 $\mathbf{M} = \begin{pmatrix} -4 \\ 2 \end{pmatrix}$ $\mathbf{N} = \begin{pmatrix} 1 & 7 \end{pmatrix}$

Work out the following.

(i) NM

.....[2]

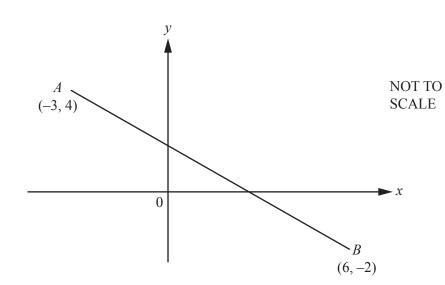
(ii) LM

(iii) L²

(iv) L^{-1} [2]



10 (a)



14

Calculate the length of *AB*.

.....[3]

(b) The point P has co-ordinates (10, 12) and the point Q has co-ordinates (2, -4).

Find

(i) the co-ordinates of the mid-point of the line PQ,

(.....)[2]

(ii) the gradient of the line PQ,

(iii) the equation of a line perpendicular to PQ that passes through the point (2, 3).

3rd term

4th term

5th term

6th term

		А	0	1	4	9	16					
		В	4	5	6	7	8					
		С	-4	-4	-2	2	8					
(a)	Complete the table.											
(b)												
	(i) sequence A,											
	[2]											
	(ii) sequence <i>B</i> . [2]											
<i>.</i>												
(c)	Find tl	he value	e of <i>n</i> when the	ne <i>n</i> th term o	f sequence A	is 576.						
							n =		[2]			
(d)	(i) F	Find an e	expression fo	r the <i>n</i> th term	n of sequence							
	C	Give you	ır answer in i	ts simplest fo	orm.							
									[3]			
	(ii) F	Find the	value of the 3	30th term of	sequence C.							
									[2]			

11 The table shows the first five terms of sequences *A*, *B* and *C*.

1st term

2nd term

Sequence

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