



# Cambridge International AS & A Level

CANDIDATE  
NAME

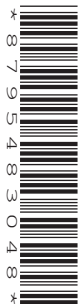
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**FURTHER MATHEMATICS**

**9231/31**

Paper 3 Further Mechanics

**October/November 2023**

**1 hour 30 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

## INSTRUCTIONS

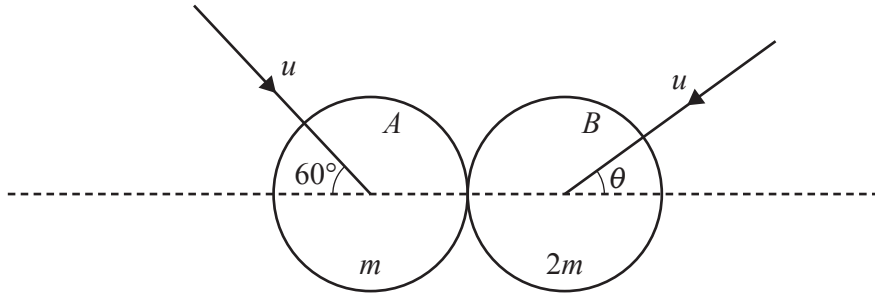
- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity ( $g$ ) is needed, use  $10 \text{ ms}^{-2}$ .

## INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Any blank pages are indicated.

1



Two uniform smooth spheres  $A$  and  $B$  of equal radii have masses  $m$  and  $2m$  respectively. The two spheres are moving with equal speeds  $u$  on a smooth horizontal surface when they collide. Immediately before the collision,  $A$ 's direction of motion makes an angle of  $60^\circ$  with the line of centres, and  $B$ 's direction of motion makes an angle  $\theta$  with the line of centres (see diagram). The coefficient of restitution between the spheres is  $e$ .

After the collision, the component of the velocity of  $A$  along the line of centres is  $v$  and  $B$  moves perpendicular to the line of centres. Sphere  $A$  now has twice as much kinetic energy as sphere  $B$ .

- (a) Show that  $v = \frac{1}{2}u(4 \cos \theta - 1)$ . [1]

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- (b) Find the value of  $\cos \theta$ . [4]

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