



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
General Certificate of Education
Advanced Subsidiary Level and Advanced Level

MATHEMATICS

9709/13

Paper 1 Pure Mathematics 1 (P1)

October/November 2010

1 hour 45 minutes

Additional Materials: Answer Booklet/Paper
Graph Paper
List of Formulae (MF9)



READ THESE INSTRUCTIONS FIRST

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 75.

Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

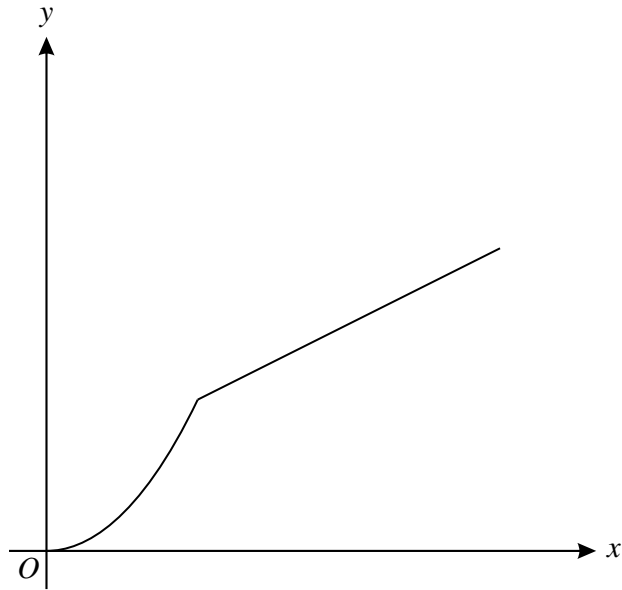
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This document consists of **5** printed pages and **3** blank pages.



- 1 Find the term independent of x in the expansion of $\left(x - \frac{1}{x^2}\right)^9$. [3]
- 2 Points A , B and C have coordinates $(2, 5)$, $(5, -1)$ and $(8, 6)$ respectively.
- (i) Find the coordinates of the mid-point of AB . [1]
- (ii) Find the equation of the line through C perpendicular to AB . Give your answer in the form $ax + by + c = 0$. [3]
- 3 Solve the equation $15 \sin^2 x = 13 + \cos x$ for $0^\circ \leq x \leq 180^\circ$. [4]
- 4 (i) Sketch the curve $y = 2 \sin x$ for $0 \leq x \leq 2\pi$. [1]
- (ii) By adding a suitable straight line to your sketch, determine the number of real roots of the equation
- $$2\pi \sin x = \pi - x.$$
- State the equation of the straight line. [3]
- 5 A curve has equation $y = \frac{1}{x-3} + x$.
- (i) Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$. [2]
- (ii) Find the coordinates of the maximum point A and the minimum point B on the curve. [5]
- 6 A curve has equation $y = f(x)$. It is given that $f'(x) = 3x^2 + 2x - 5$.
- (i) Find the set of values of x for which f is an increasing function. [3]
- (ii) Given that the curve passes through $(1, 3)$, find $f(x)$. [4]

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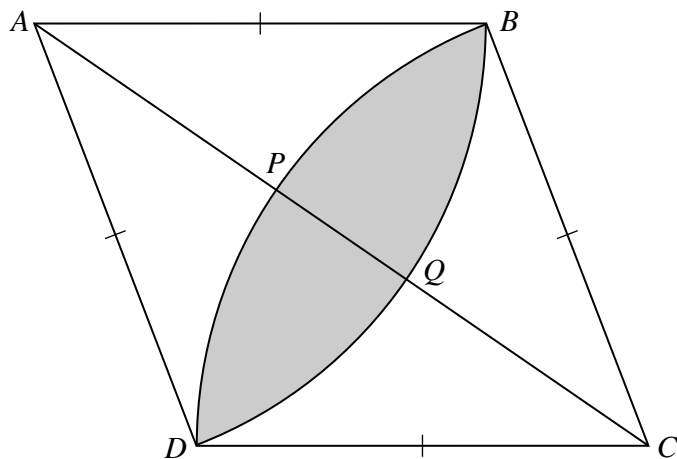


The diagram shows the function f defined for $0 \leq x \leq 6$ by

$$\begin{aligned} x &\mapsto \frac{1}{2}x^2 && \text{for } 0 \leq x \leq 2, \\ x &\mapsto \frac{1}{2}x + 1 && \text{for } 2 < x \leq 6. \end{aligned}$$

- (i) State the range of f . [1]
- (ii) Copy the diagram and on your copy sketch the graph of $y = f^{-1}(x)$. [2]
- (iii) Obtain expressions to define $f^{-1}(x)$, giving the set of values of x for which each expression is valid. [4]

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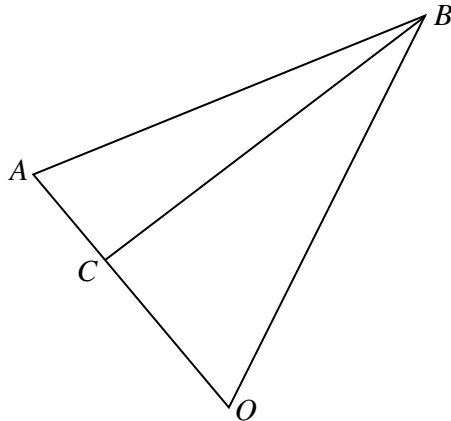


The diagram shows a rhombus $ABCD$. Points P and Q lie on the diagonal AC such that BPD is an arc of a circle with centre C and BQD is an arc of a circle with centre A . Each side of the rhombus has length 5 cm and angle $BAD = 1.2$ radians.

- (i) Find the area of the shaded region $BPDQ$. [4]
- (ii) Find the length of PQ . [4]

- 9 (a) A geometric progression has first term 100 and sum to infinity 2000. Find the second term. [3]
- (b) An arithmetic progression has third term 90 and fifth term 80.
- (i) Find the first term and the common difference. [2]
- (ii) Find the value of m given that the sum of the first m terms is equal to the sum of the first $(m + 1)$ terms. [2]
- (iii) Find the value of n given that the sum of the first n terms is zero. [2]

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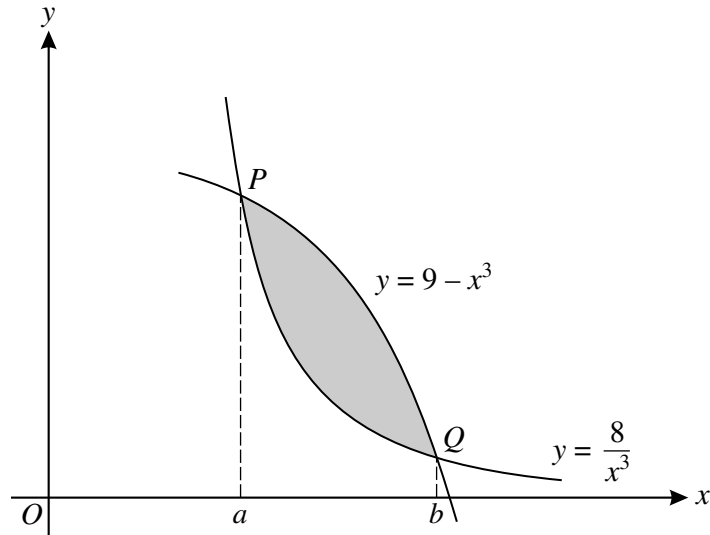
The diagram shows triangle OAB , in which the position vectors of A and B with respect to O are given by

$$\vec{OA} = 2\mathbf{i} + \mathbf{j} - 3\mathbf{k} \quad \text{and} \quad \vec{OB} = -3\mathbf{i} + 2\mathbf{j} - 4\mathbf{k}.$$

C is a point on OA such that $\vec{OC} = p\vec{OA}$, where p is a constant.

- (i) Find angle AOB . [4]
- (ii) Find \vec{BC} in terms of p and vectors \mathbf{i} , \mathbf{j} and \mathbf{k} . [1]
- (iii) Find the value of p given that BC is perpendicular to OA . [4]

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The diagram shows parts of the curves $y = 9 - x^3$ and $y = \frac{8}{x^3}$ and their points of intersection P and Q . The x -coordinates of P and Q are a and b respectively.

- (i) Show that $x = a$ and $x = b$ are roots of the equation $x^6 - 9x^3 + 8 = 0$. Solve this equation and hence state the value of a and the value of b . [4]
- (ii) Find the area of the shaded region between the two curves. [5]
- (iii) The tangents to the two curves at $x = c$ (where $a < c < b$) are parallel to each other. Find the value of c . [4]

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