

## CAMBRIDGE INTERNATIONAL MATHEMATICS

Paper 4 (Extended) MARK SCHEME Maximum Mark: 120

Published

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## Abbreviations

| awrt | answers which round to     |
|------|----------------------------|
| cao  | correct answer only        |
| dep  | dependent                  |
| FŤ   | follow through after error |
| isw  | ignore subsequent working  |
| oe   | or equivalent              |
| SC   | Special Case               |
| nfww | not from wrong working     |
| soi  | seen or implied            |
|      |                            |

| ( | Question | Answer   | Mark           | Part Marks  |
|---|----------|--|----------------|---|
| 1 | (a)      | Image at (5, 5), (7, 5), (6, 6), (5, 6)                    | 2              | If 0 scored SC1 for<br>translation $\begin{pmatrix} 3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$   |
|   | (b)      | Image at $(-1, -2)$ , $(-1, -4)$ , $(-2, -3)$ , $(-2, -2)$ | 2              | If 0 scored <b>SC1</b> for reflection in line $y = x$   |
|   | (c)      | Image at (-2, 5), (-2, 7), (-3, 5), (-3, 6)                | 3              | If 0 scored SC2 for 90° clockwise<br>about (-2, 1)<br>or SC1 for 90° anticlockwise about other<br>centre  |
|   | (d) (i)  | Enlargement<br>[scale factor] 3<br>[centre] (2, 4)         | B1<br>B1<br>B1 | If combined transformations, all three marks lost   |
|   | (ii)     | Stretch<br>[factor] 2<br>y-axis oe invariant               | B1<br>B1<br>B1 | If combined transformations, all three marks lost   |
| 2 | (a)      | $\frac{630}{9} \times 5$ and $\frac{630}{9} \times 4$ oe   | M2             | M1 for $630 \div 9$ [=70]<br>or $\frac{5 \times 630 \text{ or } 3150}{9}$ or $\frac{4 \times 630 \text{ or } 2520}{9}$  |
|   | (b) (i)  | 120  | 3              | <b>M2</b> for 98.4[0] ÷ [0].82 oe<br>or <b>M1</b> for recognising 98.4[0] is 82%  |
|   | (ii)     | 69.5 or 69.51  | 3              | M2 for $\frac{98.4[0]-30}{98.4[0]} \times 100$ oe<br>or M1 for $\frac{98.4[0]-30}{98.4[0]}$ oe or<br>$\frac{30}{98.4[0]} \times 100$<br>If 0 scored, SC1 for answer 75% |
|   | (iii)    | 211.6[0] cao final answer                                  | 1              |   |

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| Question  | Answer   | Mark      | Part Marks  |
|-----------|--|-----------|---|
| (iv)      | 183  | 4         | <b>B3</b> for answers 182.8 or 182.84 to 182.85<br>or <b>M2</b> for $150(1.02)^{10}$ seen oe<br>or <b>M1</b> for $150(1.02)^n$ seen oe<br>where $n > 1$   |
| (c)       | September or October 2035 nfww   | 5         | <b>B4</b> for 2035 or<br>19 years and 9 or 10 or 9.96 or 9.961 to<br>9.962 months nfww<br>or <b>B3</b> for 19.8 or 19.83 seen<br>or <b>M2</b> for $\frac{\log\left(\frac{500}{350}\right)}{\log(1.0015)}$ oe<br>or 350×1.0015 <sup>n</sup> = 500 <b>and</b> at least two<br>valid trials or sketch of appropriate graph<br>or <b>M1</b> for 350×1.0015 <sup>n</sup> [= 500] or<br>$350 \times \left(1 + \frac{0.15}{100}\right)^{n}$ [= 500]<br>If 0 scored <b>SC2</b> for 24[.0] or 23.95 to<br>23.98 or 2.55 or 2.552 to 2.554 seen |
| 3 (a) (i) | 60   | 1         |   |
| (ii)      | 8  | 2         | <b>B1</b> for [lq = ] 56 or [uq = ] 64  |
| (iii)     | 12   | 2         | <b>M1</b> for 188 seen  |
| (b)       | 68.6 or 68.57  | 3         | M2 for 50 $\times \frac{2.4}{1.75}$ oe<br>or M1 for <i>their</i> distance $\div$ 1.75<br>or B1 for distance = 120 or for 2.4 and<br>1.75 or 144 and 105 or 8640 and 6300<br>seen<br>If 0 scored, SC1 for 77.2 or 77.24  |
| 4 (a)     | 24   | 3         | <b>M2</b> for $6w + 5(w + 30) = 414$ oe or better<br>or <b>B1</b> for $6w$ and $5(w + 30)$ oe   |
| (b)       | $2x^2 + 4x - 7 = 0$ oe   | B2        | i.e. a correct simplified quadratic equation<br><b>M1</b> for $x^2 + (x+1)(x+3)$ [=10] oe   |
|           | Sketch of appropriate graph or correct use of formula or completing square | M1<br>dep | Dep on a quadratic from addition of two<br>areas. Must see some valid method  |
|           | 4.48 or 4.49   | B2        | <b>B1</b> for 4.484 to 4.485 or $6\sqrt{2} - 4$<br>or 1.12 or 1.121 or $1.5\sqrt{2} - 1$  |

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| Q | Question     | Answer  | Mark   | Part Marks  |
|---|--------------|---|--------|---|
| 5 | (a)          | Any 2 of the following  |        |   |
|   |              | Angle $ADX$ = Angle $BCX$ and same segment oe<br>Angle $DAX$ = Angle $CBX$ and same segment oe<br>Angle $AXD$ = Angle $BXC$ and vertically opp oe | 2      | <b>B1</b> for one of the three pairs or for at least two pairs of angles without reasons or with incorrect reasons                                |
|   | (b)          | 7.5 oe  | 2      | M1 for $\frac{2}{3} = \frac{5}{BX}$ oe  |
|   | (c)          | 67.2 or 67.20 to 67.21 nfww   | 3      | <b>M2</b> for [cos = ] $\frac{2^2 + 5^2 - 4.61^2}{2 \times 2 \times 5}$   |
|   |              |   |        | or <b>M1</b> for<br>$4.61^2 = 2^2 + 5^2 - 2 \times 2 \times 5 \cos(AXD)$  |
| 6 | (a)          | Correct sketch  |        |   |
|   |              |   | 2      | M1 for shape i.e. starting at origin then<br>one maximum then one minimum<br>A1 for two zeros to right of $x = 10$ and to<br>the left of $x = 20$ |
|   | (b)          | 13.4 or 13.41 to 13.42<br>19[.0] or 18.97   | 1<br>1 |   |
|   | (c)          | (9.49, 1) or (9.486 to 9.487, 1)  | B1 B1  |   |
|   | ( <b>d</b> ) | (16.4, -1) or (16.43, -1)   | B1 B1  |   |
|   | (e)          | $-1 \leq f(x) \leq 1$   | 1      |   |
|   | ( <b>f</b> ) | Correct sketch of parabola shape from   | B1     |   |
|   |              | approximately $y = -1$<br>5.48 or 5.477   | B1     |   |
| 7 | (a) (i)      | 576 or 575.8 to 576.0   | 3      | <b>M1</b> for $\frac{2}{3}\pi \times 5^3$ (262 or 261.7 to 261.8)   |
|   |              |   |        | <b>M1</b> for $\frac{1}{3}\pi \times 5^2 \times 12$ (314 or 314.1 to 314.2 )  |
|   | (ii)         | 0.547 or 0.5470 to 0.5472   | 2FT    | <b>FT</b> <i>their</i> (a)(i)<br><b>M1</b> for <i>their</i> (a)(i) × 0.95 ÷ 1000  |
|   | (iii)        | 1827 or 1828  | 2FT    | <ul><li>FT with consistent units usual accuracy and truncated</li><li>M1 for 1000 ÷ <i>their</i> (a)(ii)</li></ul>                                |

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| Q | Juestion     | Answer  | Mark    | Part Marks  |
|---|--------------|---|---------|---|
|   | (iv)         | 361 or 361.2 to 361.3                                     | 4       | M1 for $2\pi \times 5^2$ (157 or 157.0 to 157.1)<br>M2 for $\pi \times 5 \times \sqrt{5^2 + 12^2}$ (204 or 204.2)<br>or M1 for $\sqrt{5^2 + 12^2}$ (13)                       |
|   | (b)          | 5.37 or 5.369   | 5       | M4 for $\sqrt{\frac{377}{\pi(1+\sqrt{10})}}$<br>or M3 for $\frac{377}{\pi(1+\sqrt{10})}$<br>or M2 for $\pi r^2 + \pi r \left(\sqrt{(3r)^2 + r^2}\right) = 377$                |
|   |              |   |         | or <b>M1</b> for $r^2 + (3r)^2$ oe  |
| 8 | (a)          | [a, b, c = ] -2, 1, 2                                     | 1, 1, 1 | In any order  |
|   |              | [d=] 0  | 1       |   |
|   | <b>(b)</b>   | - 1   | 1       |   |
|   | (c)          | - 1   | 1       |   |
|   | ( <b>d</b> ) | Parabola vertex downwards and vertex below <i>x</i> -axis | M1      |   |
|   |              | Cuts given graph in 5 places                              | A1      |   |
| 9 | (a)          | 11  | 1       |   |
|   | (b)          | $\frac{7}{23}$ oe   | 1       |   |
|   | (c)          | $\frac{110}{182}$ oe                                      | 3       | M2 for $\frac{their(a)}{their(a)+3} \times \frac{their(a)-1}{their(a)+2}$<br>or M1 for a single product of two<br>fractions with first fraction $\frac{their(a)}{their(a)+3}$ |
|   | (d)          |   | 1       |   |

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| Q  | uestion | Answer                               | Mark | Part Marks   |
|----|---------|--------------------------------------|------|--|
| 10 | (a)     | 31                                   | 2    | <b>B1</b> for $[f(7) = ]$ 12<br>or <b>M1</b> for $2(x^2 - x - 30) + 7$   |
|    | (b)     | $\frac{x-7}{2}$ oe                   | 2    | <b>M1</b> for $y - 7 = 2x$ or $x = 2y + 7$ or<br>$\frac{y}{2} = x + \frac{7}{2}$   |
|    | (c)     | (2x+13)(2x+1) final answer           | 3    | <b>B2</b> for $(2x+7+6)(2x+7-6)$ or for<br>$4x^2 + 28x + 13$<br>or <b>M1</b> for $(2x+7)^2 - 36$   |
|    | (d)     | $\frac{x+5}{x+6}$ final answer nfww  | 4    | <b>B2</b> for $(x - 6)(x + 5)$<br>or <b>SC1</b> for $(x + a)(x + b)$ where<br>ab = -30 or $a + b = -1$   |
|    |         |                                      |      | and <b>B1</b> for $(x + 6)(x - 6)$   |
| 11 | (a)     | 5.4[0] or 5.396                      | 2    | M1 for $\tan 34 = \frac{AB}{8}$ oe or better   |
|    | (b)     | 20.4 or 20.38 nfww                   | 5    | <b>B1</b> for angle $D = 146$  |
|    | (c)     | 48[.0] or 48.1 or 48.04 to 48.12 cao | 2    | M2 for $[\sin C = ] \frac{8\sin(theirD)}{19}$<br>or M1 for $\frac{8}{\sin C} = \frac{19}{\sin(theirD)}$ oe<br>A1 for $[\text{angle } C = ]$ 13.6 or 13.61 to 13.63<br>OR<br>B1 for angle $A = 56$<br>M2 for $[\sin C = ] \frac{their AB \times \sin(theirA)}{19}$<br>or M1 for $\frac{their AB}{\sin C} = \frac{19}{\sin(theirA)}$ oe<br>A1 for $[\text{angle } C = ]$ 13.6 or 13.61 to 13.63<br>M1 for<br>$0.5 \times their(a) \times 19 \times \sin(90 + their(b))$ oe |
| 12 | (a)     | $n^3$ cao                            | 1    |  |
|    | (b) (i) | 392                                  | 2    | <b>B1</b> for second differences 14, 20, 26 and 32   |
|    | (ii)    | $n^3 + n^2$ oe                       | 2    | <b>M1</b> for cubic expression but not $n^3$ or $kn^3$ only  |