

## **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

MATHEMATICS 0580/43

Paper 4 (Extended) May/June 2016

MARK SCHEME
Maximum Mark: 130

## **Published**

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## **Abbreviations**

cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

nfww not from wrong working

soi seen or implied

	Question	Answer	Mark	Part marks
1	(a) (i)	36600	3	<b>M2</b> for 6100 ÷ 2 × (2 + 7 + 3) oe or <b>M1</b> for 6100 ÷ 2 soi
	(ii)	$16\frac{2}{3}$ or 16.7 [16.66 to 16.67]	1	
	(b)	1 231 708 final answer nfww	5	M4 for 5964 × 15 + 28400 × 35 + 8236 × 18 or M3 for 5964 × 15 and 28400 × 35
				or for $5964 \times 15 + 42600 \times their$ decimal $\frac{2}{3}$
				$\times 35 + (42600 - 5964 - 42600 \times their)$ decimal $\frac{2}{3}$ ) × 18
				or <b>M2</b> for 5964 × 15 <b>or</b> 28 400 × 35
				or for $42600 \times their$ decimal $\frac{2}{3} \times 35$
				or <b>M1</b> for $0.14 \times 42600$ or $42600 \div 3 \times 2$
	(c)	27.2[0] nfww	5	<b>M2</b> for 23.80 ÷ 0.7 oe or <b>M1</b> for 23.80 associated with 70% oe
				and <b>M2</b> for <i>their</i> $(23.80 \div 0.7) \times 0.8$ or <b>M1</b> for <i>their</i> $(23.80 \div 0.7) \times 0.2$
2	(a)	$x > \frac{12}{5}$ oe final answer	2	<b>B1</b> for $\frac{12}{5}$ oe in answer with incorrect or no
				sign or M1 for one correct step e.g. $5x > 9 + 3$
	(b) (i)	(y-6)(x+3) final answer	2	M1 for $y(x+3) - 6(3+x)$ or $x(y-6) + 3(y-6)$
	(ii)	8(x+3y)(x-3y) final answer	3	M2 for $2(2x + 6y)(2x - 6y)$ or $(8x + 24y)(x - 3y)$ or $(8x - 24y)(x + 3y)$ or $4(2x - 6y)(x + 3y)$ or $4(2x + 6y)(x - 3y)$ or $(4x - 12y)(2x + 6y)$ or $(4x + 12y)(2x - 6y)$ or M1 for $8(x^2 - 9y^2)$ or $(x + 3y)(x - 3y)$

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Questi	on	Answer	Mark	Part marks
(c)		$r = \frac{1}{p+7}$ final answer nfww	4	M1 removes fraction correctly M1 collects terms in r M1 removes r as a factor from their terms in r M1dep divides by bracket to leave r and denominator simplified
3 (a)	(i)	10	1	
	(ii)	-3.4 to -3.3 and -0.4 to -0.3 and 1.6 to 1.7	3	B1 for each
(	(iii)	y = -2.3 to $-2.1$ oe y = 10 to $10.1$ oe	2	B1 for each
(b)	(i)	2, -1, 4	3	B1 for each
	(ii)	Fully correct curve drawn	4	SC3 for correct curves but branches joined or touching <i>y</i> -axis
				or <b>B2FT</b> for 8 or 9 correct plots or <b>B1FT</b> for 6 or 7 correct plots
				and <b>B1</b> indep for two separate branches not touching or crossing <i>y</i> - axis
(	(iii)	−3.4 to −3.2 and 1.8 to 1.9	2	B1 for each
(c)		3.2 oe	2FT	FT $2 \div their(a)(i) + 3$ M1 for $f(-2) = 10$ or $their(a)(i)$ used
(d)		1	1	
4 (a)	(i)	$0.0025 \text{ or } \frac{1}{400} \text{ oe}$	2	<b>M1</b> for $0.05^2$ oe
	(ii)	$0.9975 \text{ or } \frac{399}{400} \text{ oe}$	1FT	<b>FT</b> for 1 – ( <i>their</i> (a)(i)) oe
(b)		0.171 or 0.1714 to 0.1715 or $\frac{6859}{40000}$	3	<b>M2</b> for $4(0.05 \times 0.95^3)$ oe
				M1 for $0.05 \times 0.95^3$ oe seen or for the 4 combinations correctly identified

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Ç	Question	Answer	Mark	Part marks
	(c)	376 nfww	4	M1 for midpoints soi (condone 1 error or omission) (225, 275, 325, 375, 425, 475) and M1 for use of $\Sigma fx$ with $x$ in correct interval including both boundaries (condone 1 further error or omission) and M1 (dependent on second M) for $\Sigma fx \div 200$
	(d) (i)	16	1	
	(ii)	33	2	<b>M1</b> for $0.8 \times 50 + 0.26 \times 100$
5	(a) (i)	275	2	<b>M1</b> for 360 – 40 – 45 oe
	(ii)	095	2FT	FT their (a) – 180 M1 for their (a) – 180 oe or 180 – 40 – 45
	(b)	464.66 to 464.67 [= 464.7]	4	M2 for $510^2 + 720^2 - 2 \times 510 \times 720 \cos 40$ or M1 for correct implicit equation A1 for 215 900 to 215 920
	(c)	44.9 or 44.86 to 44.87	3	M2 for $\frac{510\sin(40)}{464.7}$ or M1 for correct implicit equation
6	(a) (i)	Correct image $(2, -5) (4, -5) (4, -1)$	2	SC1 for reflection in $y = 0$ or 3 correct points not joined
	(ii)	Correct image (-2, 1) (-6, 1) (-6, -1)	2	SC1 for rotation 90 clockwise any centre or 3 correct points not joined
	(iii)	Translation by $\begin{pmatrix} 1 \\ 9 \end{pmatrix}$	2	B1 for each
	(iv)	Enlargement [SF] – ½ oe [Centre] (2, 1)	1 1 1	
	(b) (i)	$ \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} $	2	<b>B1</b> for one correct row or column but not the identity matrix
	(ii)	Reflection $x = 0$ oe	1 1	

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Question	Answer	Mark	Part marks
7 (a) (i)	$\frac{12}{x-1} - \frac{10}{x} = 0.5 \text{ oe}$	M2	M1 for $\frac{12}{x-1}$ or $\frac{10}{x}$
	12x - 10(x - 1) = 0.5x(x - 1) or better	M1	<b>FT</b> $\frac{10}{x} - \frac{12}{x-1} = 0.5$ only
	Brackets expanded $x^2 - 5x - 20 = 0$ with no errors or omissions seen	A1	Dep on M3 and brackets expanded
(ii)		B1	Seen anywhere or $(x - \frac{5}{2})^2$ oe
	$\sqrt{(-5)^2 - 4(1)(-20)}$ or better $p = -(-5), r = 2(1)$ or better	B1	Must be in the form $\frac{p+\sqrt{q}}{r}$ or $\frac{p-\sqrt{q}}{r}$
			or for $\frac{5}{2} + \sqrt{\left(\frac{5}{2}\right)^2 + 20}$ or $\frac{5}{2} - \sqrt{\left(\frac{5}{2}\right)^2 + 20}$
	– 2.62, 7.62 final answers	B1B1	SC1 for - 2.6 or - 2.623 to - 2.624 and 7.6 or 7.623 to 7.624 or -2.62 and 7.62 seen in working or answers 2.62 and - 7.62
(iii)	1 [ hr] 49 [mins]	2FT	FT $12 \div (their + ve \text{ root} - 1)$ or $0.5 + 10 \div (their 7.62)$ in hrs and mins, rounded to nearest min M1 for $12 \div (their + ve \text{ root} - 1)$ or $0.5 + 10 \div (their 7.62)$
(b) (i)	2.5	1	, ,
(ii)	1312.5 final answer	3	M2 for any complete correct method e.g $25 \times 10 \div 2 + 45 \times 25 + 5 \times 25 \div 2$ M1 for any correct method for a relevant area under the graph
8 (a) (i)	Not possible	1	
(ii)	$ \begin{pmatrix} 4 & 0 \\ -2 & 10 \\ 6 & -8 \end{pmatrix}  final answer $	1	
(iii)	$\begin{pmatrix} 14 & 35 \\ -8 & -20 \end{pmatrix} $ final answer	2	M1 for one correct column or row
(iv)	(-6) final answer	2	<b>M1</b> for 14 – 20
(v)	$\begin{pmatrix} -2 & 18 \\ -6 & 22 \end{pmatrix} $ final answer	2	M1 for one correct column or row

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Q	uestion	Answer	Mark	Part marks
	(b)	$\frac{1}{8} \begin{pmatrix} 5 & -3 \\ 1 & 1 \end{pmatrix}$ or better isw	2	<b>B1</b> for $k \begin{pmatrix} 5 & -3 \\ 1 & 1 \end{pmatrix}$ seen or implied, $k \neq 0$ or $\frac{1}{8} \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ seen
9	(a)	270 or 270.17 to 270.22	3	<b>M2</b> for $\frac{360-145}{360} \times \pi 12^2$ oe or <b>B1</b> for 215 seen or <b>M1</b> for $\frac{\theta}{360} \times \pi 12^2$ used
	(b)	518 or 517.6 to 517.8 nfww	6	<b>B4</b> for vertical height = 9.62 to 9.63 or <b>B3</b> for radius = 7.166 to 7.17 or <b>B2</b> for length of sector = 45.[0] or 45.02 to 45.04 or <b>M1</b> for $\frac{360-145}{360} \times 2 \times \pi \times 12$ oe or for $\sqrt{12^2 - their \ radius^2}$ and <b>M1</b> indep for $\frac{1}{3}\pi \times their \ radius^2 \times their \ h$ $(h \neq 12 \text{ or } r \neq 12)$
10	(a)	10 15		
		15 21		
		35 48	6	B1 for each correct entry
	(b) (i)	3	2	M1 for any correct substitution in $n^2 + 4n + p$ = number of tiles eg $2^2 + 4(2) + p = 15$
	(ii)	143	1FT	<b>FT</b> 140 + <i>their</i> (b)(i)
	(c)	$a = \frac{1}{2}$ oe $b = \frac{3}{2}$ oe nfww	5	<b>B1</b> for a correct simplified equation e.g. $a + b + 1 = 3$ , $4a + 2b + 1 = 6$ , 9a + 3b + 1 = 10 etc <b>B1</b> for a 2 <sup>nd</sup> correct simplified equation <b>M1</b> for correctly eliminating one variable for their equations in a and b <b>A1</b> for $a = \frac{1}{2}$ nfww <b>A1</b> for $b = \frac{3}{2}$ nfww

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Question	Answer	Mark	Part marks
(d) (i)	171	2FT	FT their $a \times 17^2 + their b \times 17 + 1$ M1 for their $a \times 17^2 + their b \times 17 + 1$
(ii)	673	1FT	<b>FT</b> their $(d)(i) \times 4 - 11$